

AISC
Night School

Thank you for joining our live webinar today.
We will begin shortly. Please standby.

Thank you.

Need Help?
Call ReadyTalk Support: 800.843.9166

AISC
Night School

Today's audio will be broadcast through the internet.

Alternatively, to hear the audio through the phone, dial 800 381 7839.

There's always a solution in Steel





Today's live webinar will begin shortly.
Please standby.
As a reminder, all lines have been muted. Please type any questions or comments through the Chat feature on the left portion of your screen.

Today's audio will be broadcast through the internet.
Alternatively, to hear the audio through the phone, dial
800 381 7839.



There's always a solution in Steel



AISC is a Registered Provider with The American Institute of Architects Continuing Education Systems (AIA/CES). Credit(s) earned on completion of this program will be reported to AIA/CES for AIA members. Certificates of Completion for both AIA members and non-AIA members are available upon request.

This program is registered with AIA/CES for continuing professional education. As such, it does not include content that may be deemed or construed to be an approval or endorsement by the AIA of any material of construction or any method or manner of handling, using, distributing, or dealing in any material or product.

Questions related to specific materials, methods, and services will be addressed at the conclusion of this presentation.



There's always a solution in Steel



Copyright Materials

This presentation is protected by US and International Copyright laws. Reproduction, distribution, display and use of the presentation without written permission of AISC is prohibited.

© The American Institute of Steel Construction 2014



There's always a solution in Steel



Course Description

Vertical Bracing Connections – Corner Connection Part 1: Wind and Low-Seismic Systems

October 20, 2014

The various steps and methodologies used for design will be highlighted as the presenter works through a design example of corner connection. Practical design tips will be discussed as well as addressing common design challenges.



There's always a solution in Steel





Learning Objectives

- Become familiar with various methodologies for bracing connection design.
- Develop an understanding of the limit states that must be reviewed for the design of bracing connections.
- Gain an understanding of the bracing connection design process through the presentation of a design example.
- Become familiar with practical design tips and how to apply to common design challenges.



Bracing Connections and Related Topics Session 4: Vertical Bracing Connections – Corner Connection Part 1: Wind and Low- Seismic Systems



Presented by
William A. Thornton, Ph.D., P.E.
Corporate Consultant to Cives Corporation
Roswell, GA

There's always a solution in steel.



Bracing Connections and Related Topics

By: William Thornton



There's always a solution in steel

Course Outline

1. Basic Principles
2. Uniform Force Method
3. Bracing Connection Details and Prying Action
- 4. Vertical Bracing Connections – Corner Part 1**
5. Vertical Bracing Connections – Corner Part 2
6. Chevron Gussets for Wind or Low-Seismic
7. Chevron Gussets for High Seismic
8. Additional Connection Topics



There's always a solution in steel

10



Session Outline

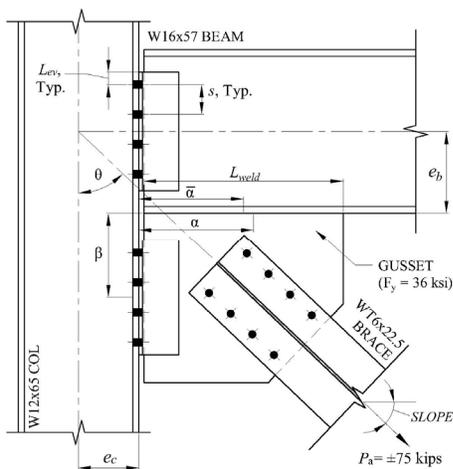
- Example of VB Corner Connection in Wind and Low-Seismic Systems
 - Begin with the brace-to-gusset design
 - Determine gusset dimensions based on brace-to-gusset connection
 - Check gusset-to-column connection
 - Check gusset-to-beam connection
 - Check beam-to-column connection



There's always a solution in steel

11

Example of VB Corner Connection (Part I) in Wind and Low-Seismic



There's always a solution in steel

12

Example of VB Corner Connection (Part I) in Wind and Low-Seismic

Given:

1. AISC 14th Edition, ASD
2. Beam-to-Column and Gusset-to-Column: $n = 4$
3. $L_{weld} = 20$ in. min. (gusset to beam) with $\frac{1}{4}$ " min. weld
4. $\frac{3}{4}$ " dia. A325-N, STD holes, UNO
5. Double L4x4x $\frac{3}{8}$ " Gr. 36 angles, horizontal SSLT with $L_{ev} = 1.25$ in. minimum and bolt spacing, $s = 3$ in.
6. Brace force, $P_a = \pm 75$ kips with slope = 43.6° , $\theta = 46.4^\circ$
7. $\frac{3}{8}$ " Gusset PL (A36), $F_y = 36$ ksi
8. WT and W Shapes ASTM A992, $F_y = 50$ ksi



There's always a solution in steel

13

Example VB Corner Connection, I Brace-to-Gusset (cont.)



There's always a solution in steel

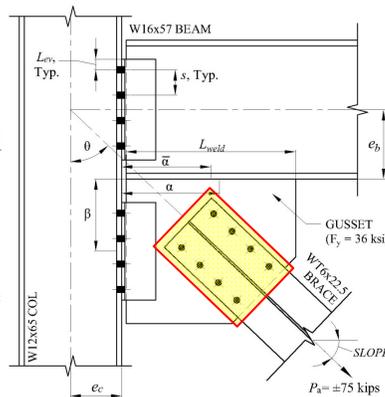
14



Example VB Corner Connection, I Brace-to-Gusset (cont.)

The example will begin with designing the brace-to-gusset connection. This will help set the geometry of the gusset.

- Determine the number of bolts required to attach the brace to the gusset
- Check gross and net tension and block shear for the brace
- Check bolt bearing and tearout of brace and gusset
- Check block shear and Whitmore tension and buckling for the gusset



There's always a solution in steel

15

Example VB Corner Connection, I Brace-to-Gusset (cont.)

Brace-to-Gusset – Bolt Shear:

AISC Manual Table 7-1

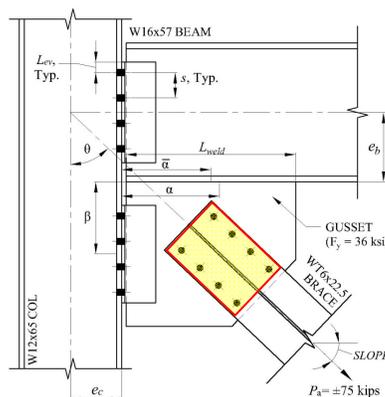
$$R_b/\Omega = nr_v/\Omega \text{ (single shear)}$$

$$= 8 \times 11.9 \text{ kips/bolt}$$

$$= 95.2 \text{ kips} \geq 75 \text{ kips o.k.}$$

Table 7-1
Available Shear
Strength of Bolts, kips

Nominal Bolt Diameter, d, in.		5/8		3/4		7/8		1				
Nominal Bolt Area, in. ²		0.307		0.442		0.601		0.785				
ASTM Desig.	Thread Cond.	F _u /Ω (ksi)		Load-ing	F _y /Ω		F _y /Ω		F _y /Ω			
		ASD	LRFD		ASD	LRFD	ASD	LRFD	ASD	LRFD		
Group A	N	27.0	40.5	S	8.29	12.4	11.9	17.9	16.2	24.3	21.2	31.8
	D	16.8	24.9	D	23.9	35.8	32.5	48.7	42.4	63.6	55.8	84.6
Group A	X	34.0	51.0	S	10.4	15.7	15.0	22.5	20.4	30.7	26.7	40.0
	D	20.9	31.3	D	30.1	45.1	40.9	61.3	53.4	80.1	70.1	105.0



There's always a solution in steel

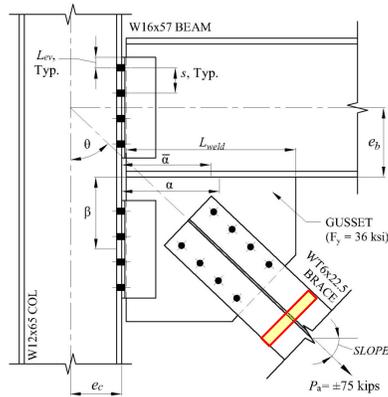
16

Example VB Corner Connection, I Brace-to-Gusset (cont.)

Brace-to-Gusset – WT Gross Tension:

AISC Specification Eq. J4-1

$$\begin{aligned} \frac{R_n}{\Omega} &= \frac{F_y A_g}{\Omega} \\ &= \frac{(50 \text{ ksi})(6.56 \text{ in.}^2)}{1.67} \\ &= 196 \text{ kips} > 75 \text{ kips o.k.} \end{aligned}$$



There's always a solution in steel

17

Net Tension

- The determination of the net section strength must account for
 - the area reduction due to the holes
 - shear lag effects
- The width of the holes is taken as $1/16$ " greater than the nominal dimension of the hole. (Spec. D3.2)
- The shear lag factor, U , is computed using Table D3.1.



There's always a solution in steel

18

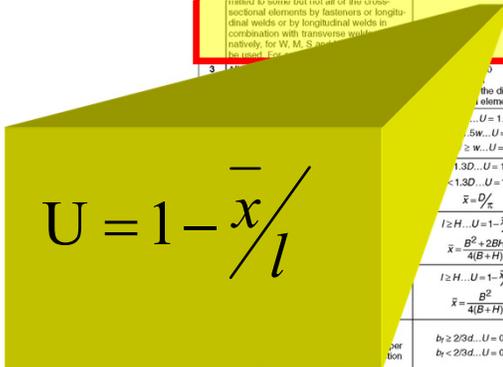
TABLE D3.1 Shear Lag Factors for Connections to Tension Members			
Case	Description of Element	Shear Lag Factor, U	Example
1	All tension members where the tension load is transmitted directly to each of the cross-sectional elements by fasteners or welds (except as in Cases 4, 5 and 6).	$U = 1.0$	—
2	All tension members, except plates and HSS, where the tension load is transmitted to some but not all of the cross-sectional elements by fasteners or longitudinal welds or by longitudinal welds in combination with transverse welds. (Alternatively, for W, M, S and HP, Case 7 may be used. For angles, Case 6 may be used.)	$U = 1 - \bar{x}/l$	
3	load is transmitted only by transverse welds to some but not all of the cross-sectional elements	and A_n = area of the directly connected elements	—
4	Plates where the tension load is transmitted by longitudinal welds only.	$l \geq 2w... U = 1.0$ $2w > l \geq 1.5w... U = 0.87$ $1.5w > l \geq w... U = 0.75$	
5	Round HSS with a single concentric gusset plate	$l \geq 1.3D... U = 1.0$ $D \leq l < 1.3D... U = 1 - \bar{x}/l$ $\bar{x} = D/2$	
6	Rectangular HSS with a single concentric gusset plate	$l \geq H... U = 1 - \bar{x}/l$ $\bar{x} = \frac{B^2 + 2BH}{4(B + H)}$	
	with two side gusset plates	$l \geq H... U = 1 - \bar{x}/l$ $\bar{x} = \frac{B^2}{4(B + H)}$	
7	W, M, S or HP Shapes or Tees cut from these shapes. (If U is calculated per Case 2, the larger value is permitted to be used.)	with flange connected with 3 or more fasteners per line in the direction of loading $b_f \geq 2/3d... U = 0.90$ $b_f < 2/3d... U = 0.85$	—
	with web connected with 4 or more fasteners per line in the direction of loading	$U = 0.70$	—
8	Single and double angles (If U is calculated per Case 2, the larger value is permitted to be used.)	with 4 or more fasteners per line in the direction of loading $U = 0.80$	—
	with 3 fasteners per line in the direction of loading (With fewer than 3 fasteners per line in the direction of loading, use Case 2.)	$U = 0.60$	—

l = length of connection, in. (mm); w = plate width, in. (mm); \bar{x} = eccentricity of connection, in. (mm); B = overall width of rectangular HSS member, measured 90° to the plane of the connection, in. (mm); H = overall height of rectangular HSS member, measured in the plane of the connection, in. (mm).

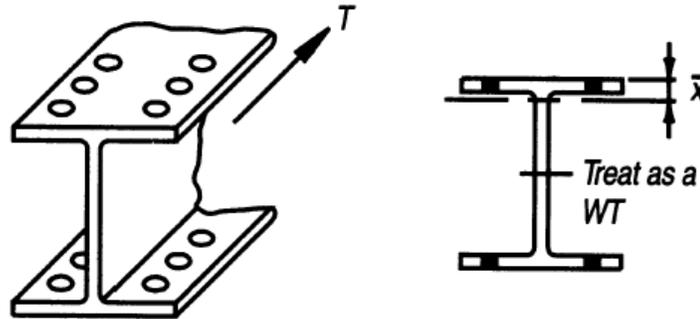


TABLE D3.1 Shear Lag Factors for Connections to Tension Members			
Case	Description of Element	Shear Lag Factor, U	Example
1	All tension members where the tension load is transmitted directly to each of the cross-sectional elements by fasteners or welds (except as in Cases 4, 5 and 6).	$U = 1.0$	—
2	All tension members, except plates and HSS, where the tension load is transmitted to some but not all of the cross-sectional elements by fasteners or longitudinal welds or by longitudinal welds in combination with transverse welds. (Alternatively, for W, M, S and HP, Case 7 may be used. For angles, Case 6 may be used.)	$U = 1 - \bar{x}/l$	
3	load is transmitted only by transverse welds to some but not all of the cross-sectional elements	and A_n = area of the directly connected elements	—
4	Plates where the tension load is transmitted by longitudinal welds only.	$l \geq 2w... U = 1.0$ $2w > l \geq 1.5w... U = 0.87$ $1.5w > l \geq w... U = 0.75$	
5	Round HSS with a single concentric gusset plate	$l \geq 1.3D... U = 1.0$ $D \leq l < 1.3D... U = 1 - \bar{x}/l$ $\bar{x} = D/2$	
6	Rectangular HSS with a single concentric gusset plate	$l \geq H... U = 1 - \bar{x}/l$ $\bar{x} = \frac{B^2 + 2BH}{4(B + H)}$	
	with two side gusset plates	$l \geq H... U = 1 - \bar{x}/l$ $\bar{x} = \frac{B^2}{4(B + H)}$	
7	W, M, S or HP Shapes or Tees cut from these shapes. (If U is calculated per Case 2, the larger value is permitted to be used.)	with flange connected with 3 or more fasteners per line in the direction of loading $b_f \geq 2/3d... U = 0.90$ $b_f < 2/3d... U = 0.85$	—
	with web connected with 4 or more fasteners per line in the direction of loading	$U = 0.70$	—
8	Single and double angles (If U is calculated per Case 2, the larger value is permitted to be used.)	with 4 or more fasteners per line in the direction of loading $U = 0.80$	—
	with 3 fasteners per line in the direction of loading (With fewer than 3 fasteners per line in the direction of loading, use Case 2.)	$U = 0.60$	—

l = length of connection, in. (mm); w = plate width, in. (mm); \bar{x} = eccentricity of connection, in. (mm); B = overall width of rectangular HSS member, measured 90° to the plane of the connection, in. (mm); H = overall height of rectangular HSS member, measured in the plane of the connection, in. (mm).



Net Tension Determination of \bar{x}



There's always a solution in steel

Example VB Corner Connection, I Brace-to-Gusset (cont.)

Brace-to-Gusset – WT Net Tension:

AISC Specification Eq. J4-2

$$\bar{x} = 1.13 \text{ in.}$$

$$l = s(n - 1) = (3 \text{ in.})(4 - 1) = 9 \text{ in.}$$

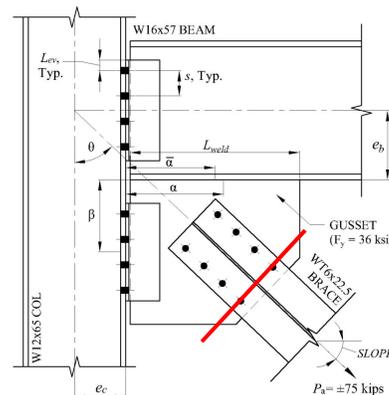
$$U = 1 - \bar{x}/l = 1 - (1.13 \text{ in.}/9 \text{ in.}) = 0.874$$

To simplify calculations:

For 3/4 in. dia. bolts with STD holes,

$$d_h = 13/16 \text{ in. and}$$

$$(d_h + 1/16 \text{ in.}) = (13/16 \text{ in.} + 1/16 \text{ in.}) = 7/8 \text{ in.}$$



There's always a solution in steel



Example VB Corner Connection, I Brace-to-Gusset (cont.)

Brace-to-Gusset – WT Net Tension (cont.):

$$A_e = U[A_g - t_f(\# \text{ lines})(d_h + 1/16 \text{ in.})]$$

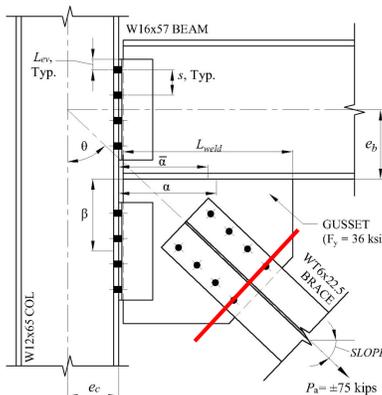
$$= 0.874 [6.56 \text{ in.}^2 - (0.575 \text{ in.})(2)(7/8 \text{ in.})]$$

$$= 4.85 \text{ in.}^2$$

$$\frac{R_n}{\Omega} = \frac{F_u A_e}{\Omega}$$

$$= \frac{(65 \text{ ksi})(4.85 \text{ in.}^2)}{2}$$

$$= 158 \text{ kips} > 75 \text{ kips o.k.}$$



There's always a solution in steel

Block Shear



There's always a solution in steel

Block Shear



A close-up photograph of a steel connection. A red box labeled "Net tension area" has an arrow pointing to the narrow section of the steel plate between two bolt holes.

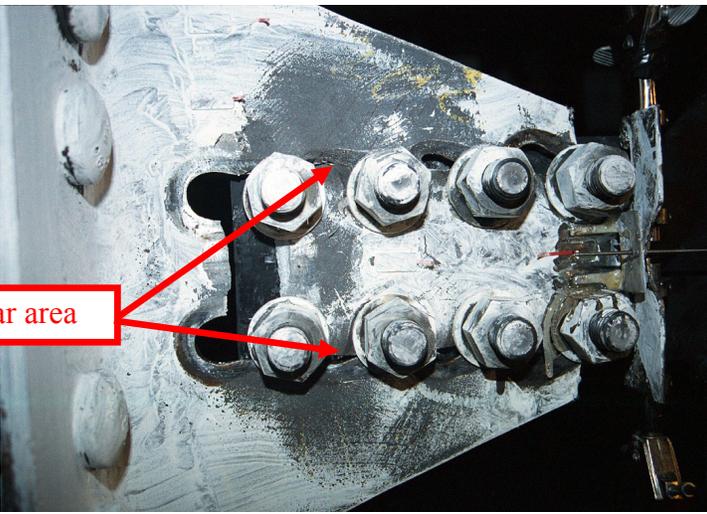
Net tension area



There's always a solution in steel

25

Block Shear



A close-up photograph of a steel connection. A red box labeled "Shear area" has two arrows pointing to the vertical faces of the steel plate between two bolt holes.

Shear area



There's always a solution in steel

26

Example VB Corner Connection, I Brace-to-Gusset (cont.)

Brace-to-Gusset – Block Shear WT:

AISC Spec Section J4.3 Block Shear Strength

$$\Omega = 2.00$$

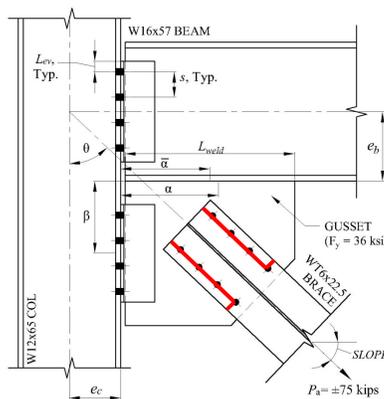
$$R_n = 0.6F_uA_{nv} + U_{bs}F_uA_{nt} \leq 0.6F_yA_{gv} + U_{bs}F_uA_{nt}$$

$$\text{Shear Rupture} = 0.6F_uA_{nv}$$

$$\text{Shear Yield} = 0.6F_yA_{gv}$$

$$\text{Tension Rupture} = F_uA_{nt}$$

$$U_{bs} = 1.0 \text{ for Direct Loaded Connections}$$



There's always a solution in steel

27

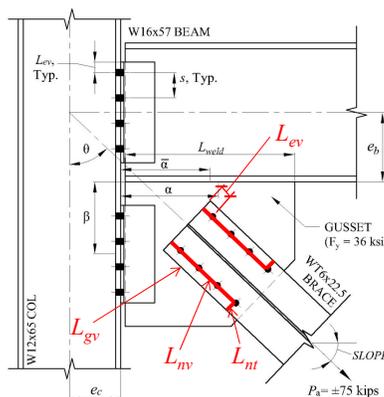
Example VB Corner Connection, I Brace-to-Gusset (cont.)

Brace-to-Gusset – Block Shear WT (cont.):

$$L_{gv} = L_{ev} + s(n - 1) = 1.5 \text{ in.} + (3 \text{ in.})(4 - 1) = 10.5 \text{ in.}$$

$$L_{nv} = L_{ev} + s(n - 1) - (n - 0.5)(d_h + 1/16 \text{ in.}) - (4 - 0.5)(7/8 \text{ in.}) = 7.44 \text{ in.}$$

$$L_{nt} = (b_f - \text{gage})/2 - (d_h + 1/16 \text{ in.})/2 = (8.05 \text{ in.} - 5.5 \text{ in.})/2 - (7/8 \text{ in.})/2 = 0.838 \text{ in.}$$



There's always a solution in steel

28

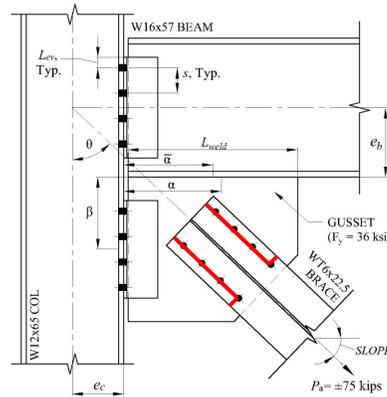
Example VB Corner Connection, I Brace-to-Gusset (cont.)

Brace-to-Gusset – Block Shear WT (cont.):

$$A_{gv} = 2L_{gv}t_f = 2(10.5 \text{ in.})(0.575 \text{ in.}) = 12.08 \text{ in.}^2$$

$$A_{nv} = 2L_{nv}t_f = 2(7.44 \text{ in.})(0.575 \text{ in.}) = 8.56 \text{ in.}^2$$

$$A_{nt} = 2L_{nt}t_f = 2(0.838 \text{ in.})(0.575 \text{ in.}) = 0.96 \text{ in.}^2$$



There's always a solution in steel

29

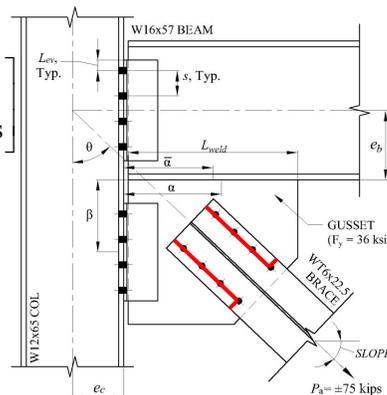
Example VB Corner Connection, I Brace-to-Gusset (cont.)

Brace-to-Gusset – Block Shear WT (cont.):

$$R_n = \min \left[\begin{array}{l} 0.6(65 \text{ ksi})(8.56 \text{ in.}^2) = 333.84 \text{ kips} \\ 0.6(50 \text{ ksi})(12.08 \text{ in.}^2) = 362.40 \text{ kips} \\ + [1(65 \text{ ksi})(0.96 \text{ in.}^2)] \end{array} \right]$$

$$= 333.84 \text{ kips} + 62.4 \text{ kips} = 396.24 \text{ kips}$$

$$R_n/\Omega = (396.24 \text{ kips})/2 = 198 \text{ kips} > 75 \text{ kips o.k.}$$



There's always a solution in steel

30

Example VB Corner Connection, I Brace-to-Gusset (cont.)

Brace-to-Gusset – Block Shear Gusset:

AISC Spec Section J4.3 Block Shear Strength

$$\Omega = 2.00$$

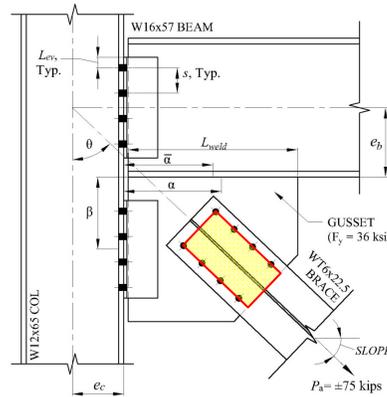
$$R_n = 0.6F_uA_{nv} + U_{bs}F_uA_{nt} \leq 0.6F_yA_{gv} + U_{bs}F_uA_{nt}$$

$$\text{Shear Rupture} = 0.6F_uA_{nv}$$

$$\text{Shear Yield} = 0.6F_yA_{gv}$$

$$\text{Tension Rupture} = F_uA_{nt}$$

$$U_{bs} = 1.0 \text{ for Direct Loaded Connections}$$



There's always a solution in steel

The lecture will skip to slide 35.

31

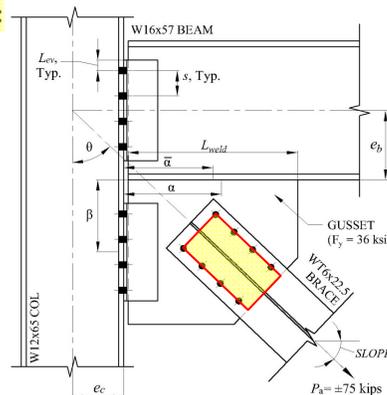
Example VB Corner Connection, I Brace-to-Gusset (cont.)

Brace-to-Gusset – Block Shear Gusset (cont.):

$$L_{gv} = L_{ev} + s(n - 1) = 1.5 \text{ in.} + (3 \text{ in.})(4 - 1) = 10.5 \text{ in.}$$

$$L_{nv} = L_{ev} + s(n - 1) - (n - 0.5)(d_h + 1/16 \text{ in.}) - (4 - 0.5)(7/8 \text{ in.}) = 7.44 \text{ in.}$$

$$L_{nt} = \text{gage} - (d_h + 1/16 \text{ in.}) = 5.5 \text{ in.} - (7/8 \text{ in.}) = 4.63 \text{ in.}$$



There's always a solution in steel

32

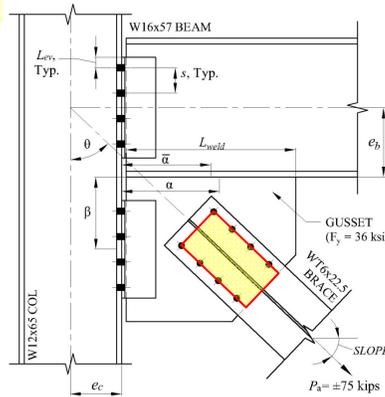
Example VB Corner Connection, I Brace-to-Gusset (cont.)

Brace-to-Gusset – Block Shear Gusset (cont.):

$$A_{gv} = 2L_{gv}t_p = 2(10.5 \text{ in.})(0.375 \text{ in.}) = 7.88 \text{ in.}^2$$

$$A_{nv} = 2L_{nv}t_p = 2(7.44 \text{ in.})(0.375 \text{ in.}) = 5.58 \text{ in.}^2$$

$$A_{nt} = L_{nt}t_p = (4.63 \text{ in.})(0.375 \text{ in.}) = 1.74 \text{ in.}^2$$



There's always a solution in steel

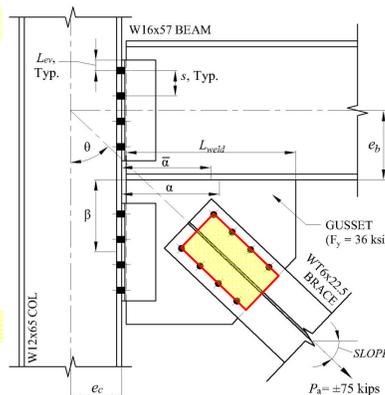
Example VB Corner Connection, I Brace-to-Gusset (cont.)

Brace-to-Gusset – Block Shear Gusset (cont.):

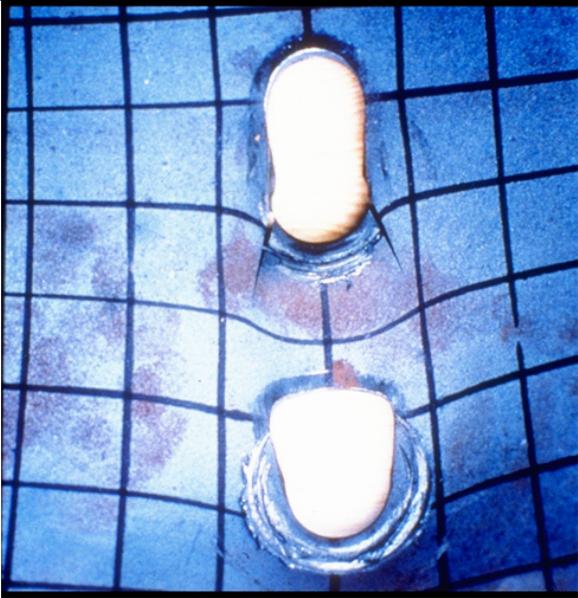
$$R_n = \min \left[\begin{array}{l} 0.6(58 \text{ ksi})(5.58 \text{ in.}^2) = 194.18 \text{ kips} \\ 0.6(36 \text{ ksi})(7.88 \text{ in.}^2) = 170.21 \text{ kips} \\ + [1(58 \text{ ksi})(1.74 \text{ in.}^2)] \end{array} \right]$$

$$= 170.21 \text{ kips} + 100.92 \text{ kips} = 271.13 \text{ kips}$$

$R_n/\Omega = (271.13 \text{ kips})/2 = 136 \text{ kips} > 75 \text{ kips}$ **o.k.**



There's always a solution in steel



Bolt Tearout

Bolt Bearing



There's always a solution in steel

35

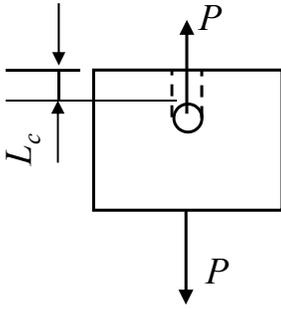
Bolt Bearing and Tearout

Bolt Tearout is easier to understand if you think about a bolt tearing through the material as shown.

There are 2 shear planes; the strength is therefore:

$$(2)(0.6)(F_u)(L_c)(t)$$

or, $1.2(F_u)(L_c)(t)$

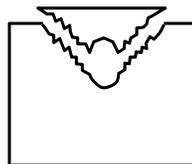


There's always a solution in steel

36

Bolt Bearing and Tearout

In reality the material will fail as shown, but test results support the equation in the *Manual*.



There's always a solution in steel

37

Bolt Bearing and Tearout

- For each bolt there are five (5) possible limit states or failure modes that need to be checked
 - Bolt Shear
 - Bolt Bearing on the Main Material
 - Bolt Bearing on the Connection Material
 - Bolt Tearout on the Main Material
 - Bolt Tearout on the Connection Material
- Then the sum of the bolt capacities can be added.



There's always a solution in steel

38

Example VB Corner Connection, I Brace-to-Gusset (cont.)

Brace-to-Gusset – Bolt Bearing/Tearout:

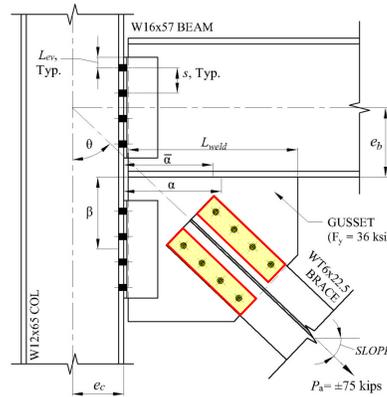
AISC Specification Eq. J3-6a

AISC Bolt Shear:

$$r_v/\Omega = 11.9 \text{ kips}$$

WT Bolt Bearing:

$$\begin{aligned} R_{brg(WT)}/\Omega &= 2.4d_b t F_u/\Omega \\ &= 2.4(0.75 \text{ in.})(0.575 \text{ in.})(65 \text{ ksi})/2 \\ &= 33.6 \text{ kips} \end{aligned}$$



There's always a solution in steel

39

Example VB Corner Connection, I Brace-to-Gusset (cont.)

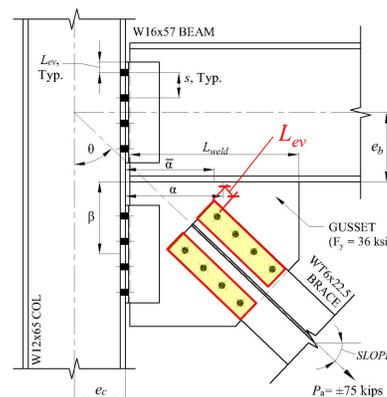
Brace-to-Gusset – Bolt Bearing (cont.):

WT Bolt Tear Out (Edge):

$$\begin{aligned} R_{tear(WT_E)}/\Omega &= 1.2[L_{ev} - (d_{h_w}/2)]t F_u/\Omega \\ &= 1.2[1.5 \text{ in.} - (1^{3/16} \text{ in.})/2] \\ &\quad \times (0.575 \text{ in.})(65 \text{ ksi})/2 \\ &= 24.5 \text{ kips} \end{aligned}$$

WT Bolt Tear Out (Center):

$$\begin{aligned} R_{tear(WT_C)}/\Omega &= 1.2(s - d_{h_w})t F_u/\Omega \\ &= 1.2(3 \text{ in.} - 1^{3/16} \text{ in.})(0.575 \text{ in.}) \\ &\quad \times (65 \text{ ksi})/2 \\ &= 49.1 \text{ kips} \end{aligned}$$



There's always a solution in steel

40

Example VB Corner Connection, I Brace-to-Gusset (cont.)

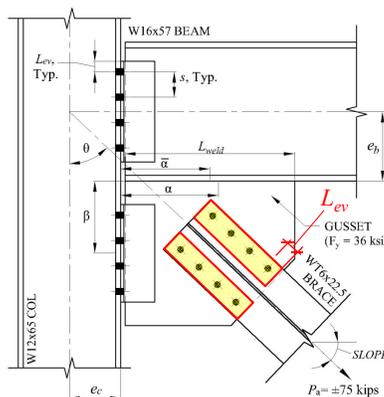
Brace-to-Gusset – Bolt Bearing (cont.):

Plate Bolt Bearing:

$$\begin{aligned} R_{brg(PL)}/\Omega &= 2.4d_b t_p F_u / \Omega \\ &= 2.4(0.75 \text{ in.})(0.375 \text{ in.})(58 \text{ ksi})/2 \\ &= 19.6 \text{ kips} \end{aligned}$$

Plate Bolt Tear Out (Edge):

$$\begin{aligned} R_{tear(PL_E)}/\Omega &= 1.2[L_{ev} - (d_h w/2)]t_p F_u / \Omega \\ &= 1.2[1.5 \text{ in.} - (13/16 \text{ in.})/2] \\ &\quad \times (0.375 \text{ in.})(58 \text{ ksi})/2 \\ &= 14.3 \text{ kips} \end{aligned}$$



There's always a solution in steel

41

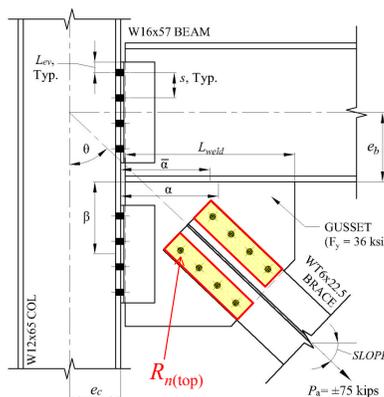
Example VB Corner Connection, I Brace-to-Gusset (cont.)

Brace-to-Gusset – Bolt Bearing (cont.):

Plate Bolt Tear Out (Center):

$$\begin{aligned} R_{tear(PL_C)}/\Omega &= 1.2(s - d_h w)t_p F_u / \Omega \\ &= 1.2(3 \text{ in.} - 13/16 \text{ in.})(0.375 \text{ in.}) \\ &\quad \times (58 \text{ ksi})/2 \\ &= 28.6 \text{ kips} \end{aligned}$$

$$\begin{aligned} R_{n(top)}/\Omega &= \min \{r_v/\Omega, R_{brg(WT)}/\Omega, R_{tear(WT_E)}/\Omega, \\ &\quad R_{brg(PL)}/\Omega, R_{tear(PL_C)}/\Omega\} \\ &= \min \{11.9 \text{ kips}, 33.6 \text{ kips}, 24.5 \text{ kips}, \\ &\quad 19.6 \text{ kips}, 28.6 \text{ kips}\} \\ &= 11.9 \text{ kips} \end{aligned}$$



There's always a solution in steel

42

Example VB Corner Connection, I Brace-to-Gusset (cont.)

Brace-to-Gusset – Bolt Bearing (cont.):

$$R_{n(\text{center})}/\Omega = \min \{ r_v/\Omega, R_{brg(\text{WT})}/\Omega, R_{tear(\text{WT_C})}/\Omega, R_{brg(\text{PL})}/\Omega, R_{tear(\text{PL_C})}/\Omega \}$$

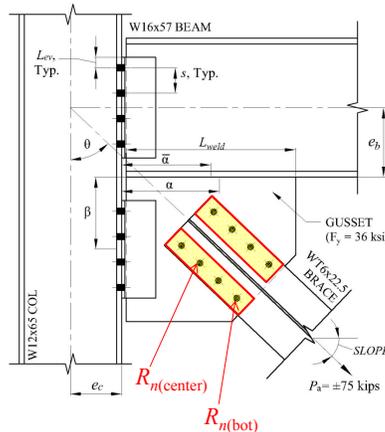
$$= \min \{ 11.9 \text{ kips}, 33.6 \text{ kips}, 49.1 \text{ kips}, 19.6 \text{ kips}, 28.6 \text{ kips} \}$$

$$= 11.9 \text{ kips}$$

$$R_{n(\text{bot})}/\Omega = \min \{ r_v/\Omega, R_{brg(\text{WT})}/\Omega, R_{tear(\text{WT_C})}/\Omega, R_{brg(\text{PL})}/\Omega, R_{tear(\text{PL_E})}/\Omega \}$$

$$= \min \{ 11.9 \text{ kips}, 33.6 \text{ kips}, 49.1 \text{ kips}, 19.6 \text{ kips}, 14.3 \text{ kips} \}$$

$$= 11.9 \text{ kips}$$



There's always a solution in steel

43

Example VB Corner Connection, I Brace-to-Gusset (cont.)

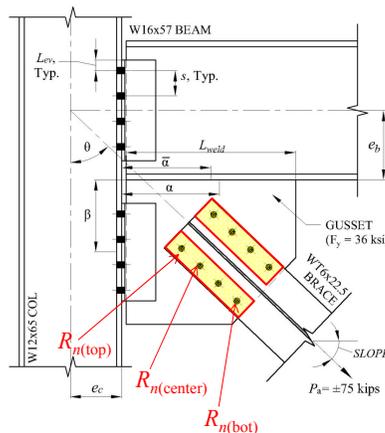
Brace-to-Gusset – Bolt Bearing (cont.):

Total Bolt Strength

$$R_n/\Omega = [R_{n(\text{top})}/\Omega + (R_{n(\text{center})}/\Omega)(n - 2) + R_{n(\text{bot})}/\Omega](2 \text{ lines})$$

$$= [11.9 \text{ kips} + (11.9 \text{ kips})(4 - 2) + 11.9 \text{ kips}](2)$$

$$= 95.2 \text{ kips} > 75 \text{ kips o.k.}$$



There's always a solution in steel

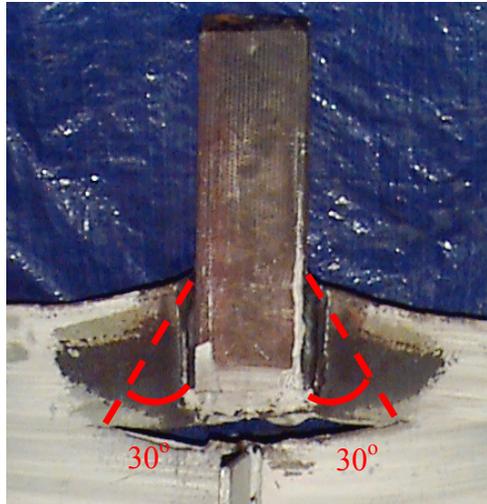
44

Whitmore Section



There's always a solution in steel

Whitmore Section



There's always a solution in steel



Example VB Corner Connection, I Brace-to-Gusset (cont.)

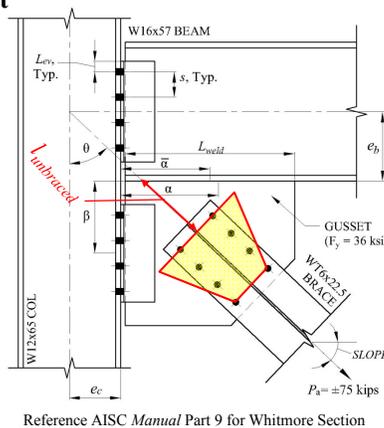
Brace-to-Gusset – Whitmore Section of Gusset Plate:

Whitmore Compression will control over Whitmore Tension by inspection.

$$l_{unbraced} = 8.81 \text{ in. max}$$

$$\begin{aligned} l_w &= 2(l_{conn})\tan 30^\circ + gage \\ &= 2(9 \text{ in.})\tan 30^\circ + 5.5 \text{ in. min.} \\ &= 15.9 \text{ in.} \end{aligned}$$

$$\begin{aligned} l_{w(\text{beam})} &= \text{length of Whitmore in beam} \\ &= 0 \text{ in. from geometric layout} \end{aligned}$$



Reference AISC Manual Part 9 for Whitmore Section



There's always a solution in steel

47

Example VB Corner Connection, I Brace-to-Gusset (cont.)

Brace-to-Gusset – Whitmore Section of Gusset Plate (cont.):

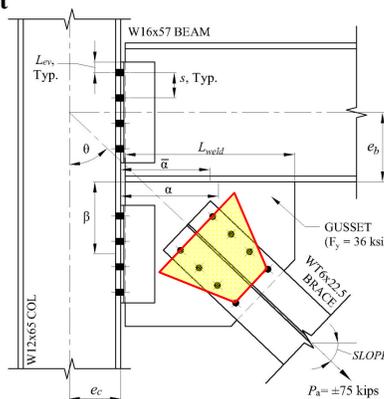
$$\begin{aligned} l_{w(\text{gusset})} &= l_w - l_{w(\text{beam})} \\ &= 15.9 \text{ in.} - 0 \text{ in.} = 15.9 \text{ in.} \end{aligned}$$

$K = 0.5$ from AISC's *Design Examples* (v14.1 is web-based and free at www.aisc.org), Example II.C-2

$$\begin{aligned} Kl_{unbraced}/r &= [0.5(8.81 \text{ in.})\sqrt{(12)}]/0.375 \text{ in.} \\ &= 40.7 \end{aligned}$$

$$\text{AISC Manual Table 4-22, } F_{cr(\text{Gr.36})}/\Omega = 19.7 \text{ ksi}$$

$$\text{AISC Manual Table 4-22, } F_{cr(\text{Gr.50})}/\Omega = 26.5 \text{ ksi}$$



There's always a solution in steel

48

Example VB Corner Connection, I Brace-to-Gusset (cont.)

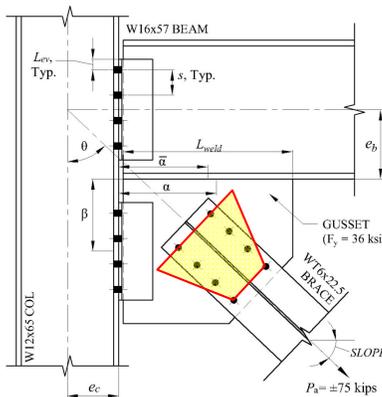
Brace-to-Gusset – Whitmore Section of Gusset
 Plate (cont.):

AISC Manual
 Table 4-22 (continued)
 Available Critical Stress for
 Compression Members

KL/r	F _y = 35 ksi		F _y = 36 ksi		F _y = 42 ksi		F _y = 46 ksi		F _y = 50 ksi		
	F _{cr} /Ω _c	φF _{cr}									
	ASD	LFRD									
41	19.2	28.9	41	19.7	29.7	41	22.7	34.1	41	24.6	37.0
42	19.2	28.8	42	19.6	29.5	42	22.6	33.9	42	24.5	36.8
43	19.1	28.7	43	19.6	29.4	43	22.5	33.7	43	24.3	36.6

From AISC *Design Examples* Example IIC-2: The effective length factor *K* has been established as 0.5 by full scale tests on bracing connections (Gross, 1990). It assumes that the gusset plate is supported on both connected edges.

(Alternately, see: Dowswell, Bo (2006), "Effective Length Factors for Gusset Plate Buckling," AISC *Engineering Journal*, 2nd Qtr.)



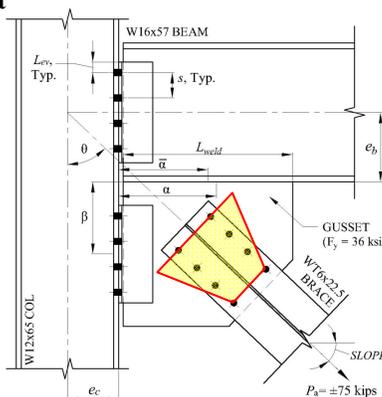
There's always a solution in steel

Example VB Corner Connection, I Brace-to-Gusset (cont.)

Brace-to-Gusset – Whitmore Section of Gusset
 Plate (cont.):

$$\begin{aligned} \frac{P_n}{\Omega_c} &= \frac{F_{cr}(\text{gusset})}{\Omega_c} A_{w(\text{gusset})} + \frac{F_{cr}(\text{beam})}{\Omega_c} A_{w(\text{beam})} \\ &= (19.7 \text{ ksi})(0.375 \text{ in.})(15.9 \text{ in.}) + 0 \\ &= 83 \text{ kips} \geq 75 \text{ kips o.k.} \end{aligned}$$

Note: for Whitmore tension, use F_y/Ω in lieu of F_{cr}/Ω



There's always a solution in steel

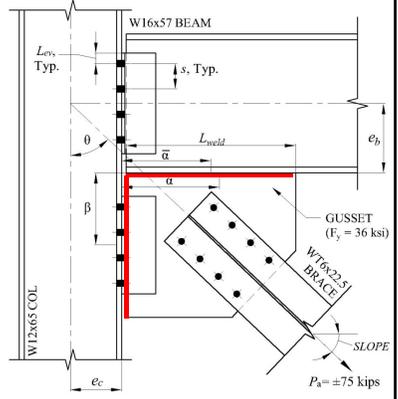
Example VB Corner Connection, I Gusset Forces



There's always a solution in steel

Example VB Corner Connection, I Gusset Forces

Next, the gusset forces, V_b , H_b , M_b , V_c , H_c , and M_c , will be determined using the Uniform Force Method.



There's always a solution in steel



Geometry of UFM

All Parts are in Equilibrium

$$\alpha - \beta \tan \theta = e_b \tan \theta - e_c$$

$$H_b = \frac{\alpha}{r} P$$

$$V_c = \frac{\beta}{r} P$$

$$V_b = \frac{e_b}{r} P$$

$$H_c = \frac{e_c}{r} P$$

$$r = \sqrt{(\alpha + e_c)^2 + (\beta + e_b)^2}$$

There's always a solution in steel

53

Example VB Corner Connection, I Gusset Forces (cont.)

Determine Gusset Forces using UFM:

$\tan \theta = 1.05$

$e_b = d_B / 2 = (16.4 \text{ in.}) / 2 = 8.2 \text{ in.}$

$e_c = d_c / 2 = (12.1 \text{ in.}) / 2 = 6.05 \text{ in.}$
 (note: $e_c = 0.0 \text{ in.}$ for connections into column web, except Special Case IV)

There's always a solution in steel

54

Example VB Corner Connection, I Gusset Forces (cont.)

Determine Gusset Forces using UFM (cont.):

$\bar{\beta}$ = distance to center of gusset-to-column connections

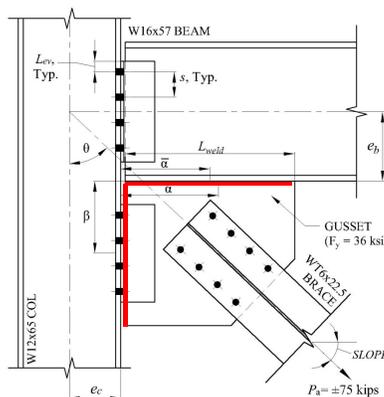
From geometric layout, $H_{gusset} = 16.875$ in.

Place bolts in approximate center of gusset,

$$\bar{\beta} = 8.5 \text{ in.}$$

Let $\beta = \bar{\beta}$

$$\begin{aligned} \alpha &= e_b \tan \theta - e_c + \beta \tan \theta \\ &= (8.2 \text{ in.})(1.05) - 6.05 \text{ in.} \\ &\quad + (8.5 \text{ in.})(1.05) \\ &= 11.5 \text{ in.} \end{aligned}$$



There's always a solution in steel

55

Example VB Corner Connection, I Gusset Forces (cont.)

Determine Gusset Forces using UFM (cont.):

$$\bar{\alpha} = \frac{L_{weld}}{2} + 0.5 \text{ in. (setback for angles)}$$

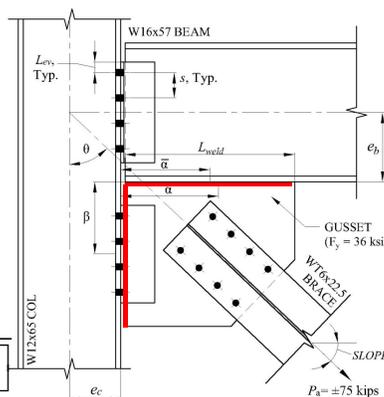
$$= \frac{20 \text{ in.}}{2} + 0.5 \text{ in.}$$

$$= 10.5 \text{ in. min.} \rightarrow \text{does not equal } \alpha$$

$$r = \sqrt{[(\alpha + e_c)^2 + (\beta + e_b)^2]}$$

$$= \sqrt{[(11.5 \text{ in.} + 6.05 \text{ in.})^2 + (8.5 \text{ in.} + 8.2 \text{ in.})^2]}$$

$$= 24.2 \text{ in.}$$



There's always a solution in steel

56

Example VB Corner Connection, I Gusset Forces (cont.)

Determine Gusset Forces using UFM (cont.):

$$V_b = P_a (e_b/r)$$

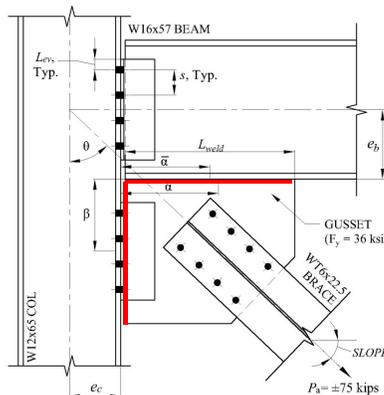
$$= (75 \text{ kips})(8.2 \text{ in.}/24.2 \text{ in.})$$

$$= 25.4 \text{ kips}$$

$$H_b = P_a (\alpha/r)$$

$$= (75 \text{ kips})(11.5 \text{ in.}/24.2 \text{ in.})$$

$$= 35.6 \text{ kips}$$



There's always a solution in steel

57

Example VB Corner Connection, I Gusset Forces (cont.)

$$M_b = V_b (\alpha - \bar{\alpha})$$

$$= 25.4 \text{ kips}(11.5 \text{ in.} - 10.5 \text{ in.})$$

$$= 25.4 \text{ kip-in.}$$

$$V_c = P_a (\beta/r)$$

$$= 75 \text{ kips}(8.5 \text{ in.}/24.2 \text{ in.})$$

$$= 26.3 \text{ kips}$$

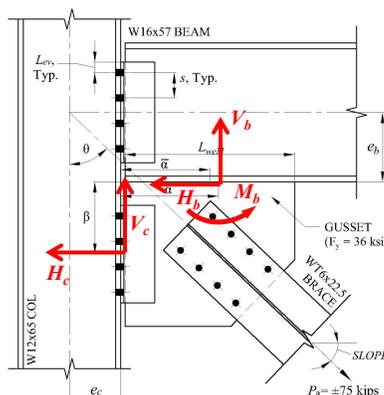
$$H_c = P_a (e_c/r)$$

$$= 75 \text{ kips}(6.05 \text{ in.}/24.2 \text{ in.})$$

$$= 18.8 \text{ kips}$$

(Note: $H_c = 0$ kips for connections to column web, except Special Case IV)

$$M_c = 0 \quad \text{since } \beta = \bar{\beta}$$



There's always a solution in steel

58

Example VB Corner Connection, I Gusset-to-Column

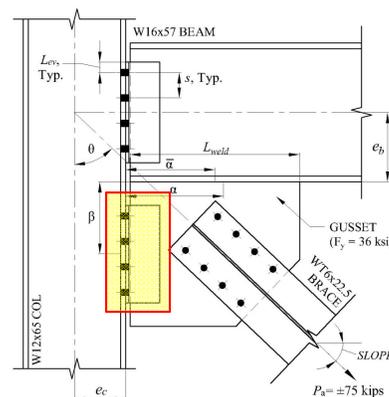


There's always a solution in steel

Example VB Corner Connection, I Gusset-to-Column

The gusset-to-column will be designed using the gusset forces previously determined.

- a. Check bolts at column flange
- b. Check prying of angles and column flange
- c. Check bolt bearing and tearout of angles and column flange
- d. Check gross and net shear and block shear for angles
- e. Check angle welds



There's always a solution in steel

Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Bolts:

$$R_b/\Omega = 2n(r_v/\Omega)$$

$$= 2(4)(11.9 \text{ kips})$$

$$= 95.2 \text{ kips} > V_c = 26.3 \text{ kips o.k.}$$

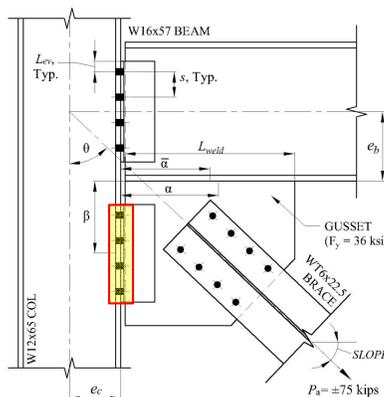
Check Shear and Tension:

$$V_{bolt} = V_c/(2n) = 26.3 \text{ kips}/[(2)(4)]$$

$$= 3.29 \text{ kips}$$

$$T_{bolt} = H_c/(2n) = 18.8 \text{ kips}/[(2)(4)]$$

$$= 2.35 \text{ kips}$$



There's always a solution in steel

Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Bolts (cont.):

Check Shear and Tension (cont.):

$$A_b = \frac{\pi d_b^2}{4}$$

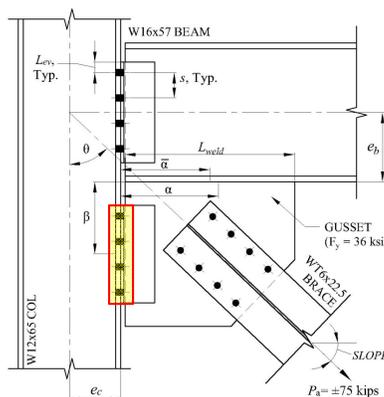
$$= \frac{3.14(0.75 \text{ in.})^2}{4}$$

$$= 0.442 \text{ in.}^2$$

$$f_{rv} = V_{bolt}/A_b$$

$$= 3.29 \text{ kips}/0.442 \text{ in.}^2$$

$$= 7.44 \text{ ksi}$$



There's always a solution in steel

Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Bolts (cont.):

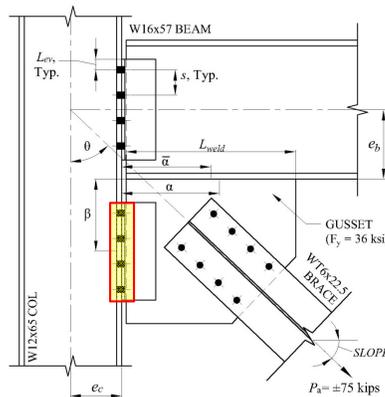
Check Shear and Tension (cont.):

$$F'_{nt} = 1.3F_{nt} - \Omega F_{nv} f_{rv} / F_{nv} \leq F_{nt} \quad (\text{Spec J3-3a})$$

$$= 1.3(90 \text{ ksi}) - 2(90 \text{ ksi})(7.44 \text{ ksi}) / (54 \text{ ksi})$$

$$= 92.2 \text{ ksi} > 90 \text{ ksi, use } 90 \text{ ksi}$$

AISC Specification TABLE J3.2 Nominal Strength of Fasteners and Threaded Parts, ksi (MPa)		
Description of Fasteners	Nominal Tensile Strength, F_{nt} , ksi (MPa) ^a	Nominal Shear Strength in Bearing-Type Connections, F_{nv} , ksi (MPa) ^b
A307 bolts	45 (310)	27 (188) ⁽⁶⁾
Group A (e.g., A325) bolts, when threads are not excluded from shear planes	90 (620)	54 (372)



There's always a solution in steel

Example VB Corner Connection, I Gusset-to-Column (cont.)

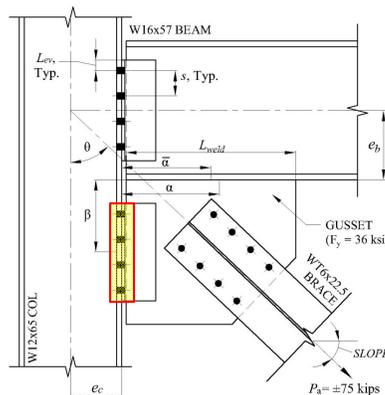
Gusset-to-Column – Bolts (cont.):

Check Shear and Tension (cont.):

$$\frac{r_t}{\Omega} = \frac{F'_{nt} A_b}{\Omega} \quad (\text{AISC Spec J3-2})$$

$$= \frac{(90 \text{ ksi})(0.442 \text{ in.}^2)}{2}$$

$$= 19.9 \text{ kips} > T_{bolt} = 2.35 \text{ kips o.k.}$$



There's always a solution in steel

Example VB Corner Connection, I Gusset-to-Column (cont.)

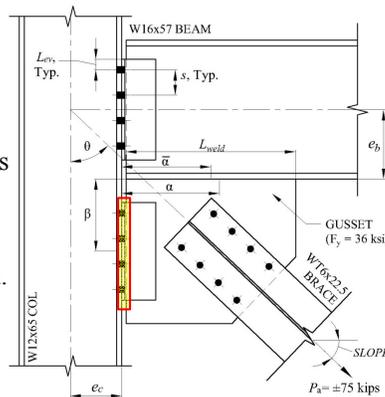
Gusset-to-Column – Prying of Angles:

For connections to column webs, there is no tension force on the angle since $H_c = 0$ kips. For this example, which is to a column flange, however:

$$T_{bolt} = H_c / (2n) = 18.8 \text{ kips} / [(2)(4)] = 2.35 \text{ kips}$$

$$b = \text{gage}/2 - t_p/2 - t_d/2 \\ = 5.5 \text{ in.}/2 - 0.375 \text{ in.}/2 - 0.375/2 = 2.38 \text{ in.}$$

$$b' = b - d_b/2 = \\ = 2.38 \text{ in.} - 0.75 \text{ in.}/2 = 2 \text{ in.}$$



There's always a solution in steel

The lecture will skip
 to slide 75.

65

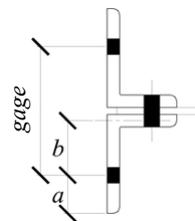
Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Prying of Angles (cont.):

$$a = [2(\text{angle OSL}) + t_p - \text{gage}] / 2 \\ = [2(4 \text{ in.}) + 0.375 \text{ in.} - 5.5 \text{ in.}] / 2 \\ = 1.44 \text{ in.}$$

$$a' = a + d_b/2 \leq 1.25b + d_b/2 \\ = 1.44 \text{ in.} + 0.75 \text{ in.}/2 \\ \leq 1.25(2.38 \text{ in.}) + 0.75 \text{ in.}/2 \\ = 1.82 \text{ in.} \leq 3.35 \text{ in.} \\ = 1.82 \text{ in.}$$

$$\rho = b' / a' = 2 \text{ in.} / 1.82 \text{ in.} = 1.10$$



There's always a solution in steel

66

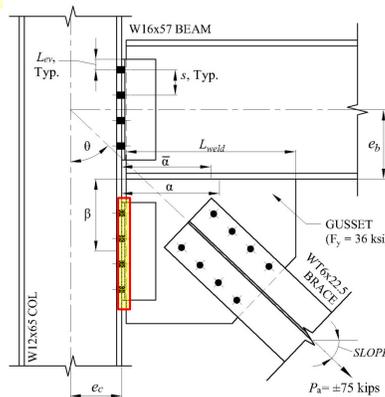
Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Prying of Angles (cont.):

$$p = L/n = 11.5 \text{ in.}/4 = 2.88 \text{ in. (tributary area per bolt)}$$

$$\delta = 1 - d'/p = 1 - 0.8125 \text{ in.}/2.88 \text{ in.} = 0.717$$

$$B = r_t/\Omega = 19.9 \text{ kips (bolt available tensile strength from previously)}$$



There's always a solution in steel

67

Example VB Corner Connection, I Gusset-to-Column (cont.)

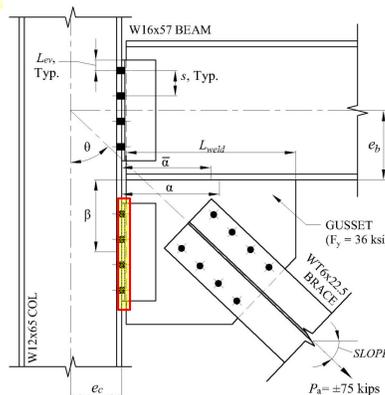
Gusset-to-Column – Prying of Angles (cont.):

$$t_c = \sqrt{\frac{\Omega 4 B b'}{p F_u}} \quad (\text{AISC Manual Eq. 9-30a})$$

$$= \sqrt{\frac{1.67(4)(19.9 \text{ kips})(2 \text{ in.})}{(2.88 \text{ in.})(58 \text{ ksi})}}$$

$$= 1.26 \text{ in.}$$

t_c = minimum thickness of angles to develop full available tensile strength of bolt with no prying



There's always a solution in steel

68

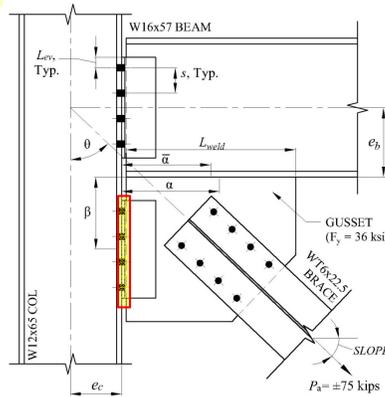
Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Prying of Angles (cont.):

$$\alpha' = \frac{1}{\delta(1+\rho)} \left[\left(\frac{t_c}{t} \right)^2 - 1 \right] \quad (\text{AISC Manual Eq. 9-35})$$

$$= \frac{1}{0.717(1+1.10)} \left[\left(\frac{1.26 \text{ in.}}{0.375 \text{ in.}} \right)^2 - 1 \right]$$

$$= 6.83 \text{ in.}$$



There's always a solution in steel

69

Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Prying of Angles (cont.):

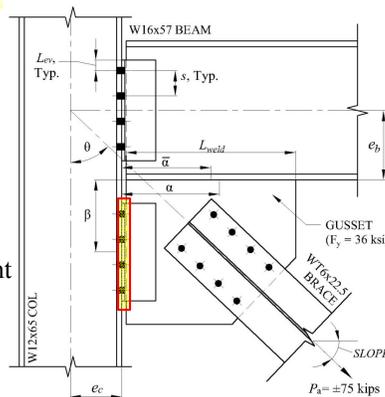
Note:

When $\alpha' < 0$, this means that the fitting has sufficient strength and stiffness to develop the full bolt available tensile strength,

$$Q = 1 \quad (\text{AISC Manual Eq. 9-32})$$

When $0 \leq \alpha' < 1$, this means that the fitting has sufficient strength and stiffness to develop the full bolt available tensile strength, but insufficient stiffness to prevent prying action,

$$Q = \left(\frac{t}{t_c} \right)^2 (1 + \delta\alpha') \quad (\text{AISC Manual Eq. 9-33})$$



There's always a solution in steel

70

Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Prying of Angles (cont.):

For the example,

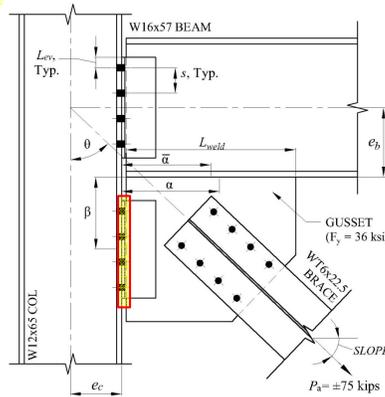
$$\alpha' = 6.83 > 1$$

This means that the angle has insufficient strength to develop the full bolt available tensile strength. Therefore,

$$Q = \left(\frac{t}{t_c}\right)^2 (1 + \delta) \quad (\text{AISC Manual Eq. 9-34})$$

$$= \left(\frac{0.375 \text{ in.}}{1.26 \text{ in.}}\right)^2 (1 + 0.717 \text{ in.})$$

$$= 0.152$$



There's always a solution in steel

71

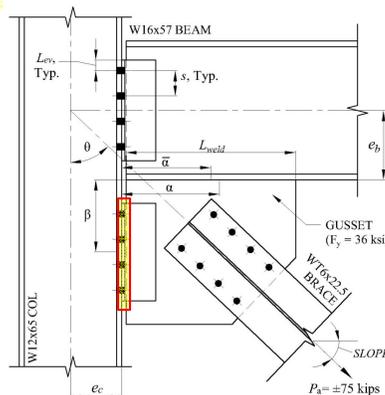
Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Prying of Angles (cont.):

The available tensile strength including the effects of prying action, T_{avail} , is:

$$T_{avail} = BQ = (19.9 \text{ kips})(0.152)$$

$$= 3.02 \text{ kips} > T_{bolt} = 2.35 \text{ kips o.k.}$$



There's always a solution in steel

72

Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Prying of Angles (cont.):

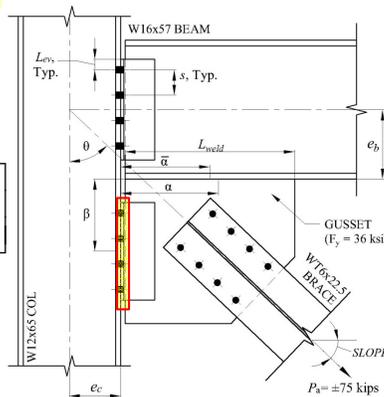
If prying force, q , needs to be determined:

$$\alpha = \left(\frac{1}{\delta} \right) \left[\frac{T}{B} \left(\frac{t_c}{t} \right)^2 - 1 \right] \quad (\text{AISC Manual Eq. 9-29})$$

$$= \left(\frac{1}{0.717} \right) \left[\left(\frac{2.35 \text{ kips}}{19.9 \text{ kips}} \right) \left(\frac{1.26 \text{ in.}}{0.375 \text{ in.}} \right)^2 - 1 \right]$$

$$= 0.465 > 0 \text{ and } < 1.0$$

Note: When $\alpha > 1$, the connection is not adequate.



There's always a solution in steel

73

Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Prying of Angles (cont.):

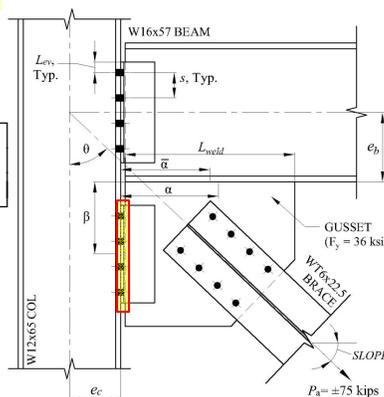
$$q = B \left[\delta \alpha \rho \left(\frac{t}{t_c} \right)^2 \right] \quad (\text{AISC Manual Eq. 9-28})$$

$$= 19.9 \text{ kips} \left[(0.717)(0.465)(1.10) \left(\frac{0.375 \text{ in.}}{1.26 \text{ in.}} \right)^2 \right]$$

$$= 0.637 \text{ kips}$$

$$B_c = T_{\text{bolt}} + q = 2.35 \text{ kips} + 0.637 \text{ kips}$$

$$= 2.99 \text{ kips} \leq B = 19.9 \text{ kips o.k.}$$



There's always a solution in steel

74

Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Prying of Column Flange:

For connections to column webs, there is no tension force on the angle since $H_c = 0$ kips. For this example, which is to a column flange, use the following criteria:

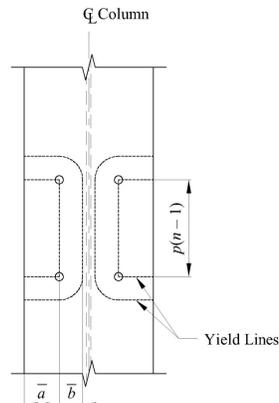
Determine effective flange width

$$p_{eff} = [p(n-1) + \pi\bar{b} + 2\bar{a}] / n$$

(Ref Akbar Tamboli, *Handbook of Steel Connection Design and Details*, 2nd Ed.)

p = spacing = 3 in.

Note: $\bar{a} = a$ and $\bar{b} = b$



(A.P. Mann and L.J. Morris, "Limit Design of Extended End-Plate Connections," *Journal of the Structural Division, ASCE*, Vol. 105, ST3, March 1979)



There's always a solution in steel

Example VB Corner Connection, I Gusset-to-Column (cont.)

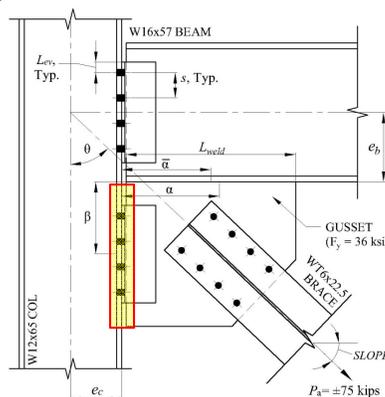
Gusset-to-Column – Prying of Column Flange (cont.):

$$\begin{aligned} \bar{b} &= (\text{gage} - t_{wc}) / 2 \\ &= (5.5 \text{ in.} - 0.39 \text{ in.}) / 2 = 2.56 \text{ in.} \end{aligned}$$

$$\begin{aligned} \bar{a} &= (b_{fc} - \text{gage}) / 2 \\ &= (12 \text{ in.} - 5.5 \text{ in.}) / 2 = 3.25 \text{ in.} \end{aligned}$$

$$\begin{aligned} p_{eff} &= [p(n-1) + \pi\bar{b} + 2\bar{a}] / n \\ &= [(3 \text{ in.})(4-1) + (3.14)(2.56 \text{ in.}) \\ &\quad + (2)(3.25 \text{ in.})] / 4 \\ &= 5.88 \text{ in.} \end{aligned}$$

Note: use 3" max if at top of column



There's always a solution in steel

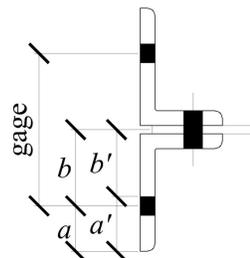
Example VB Corner Connection, I Gusset-to-Column (cont.)

**Gusset-to-Column – Prying of Column Flange
 (cont.):**

$$T_{bolt} = H_c / (2n) = 18.8 \text{ kips} / [(2)(4)] = 2.35 \text{ kips}$$

$$b = \text{gage} / 2 - t_{wc} / 2 \\ = 5.5 \text{ in.} / 2 - 0.39 \text{ in.} / 2 = 2.56 \text{ in.}$$

$$b' = b - d_b / 2 = \\ = 2.55 \text{ in.} - 0.75 \text{ in.} / 2 = 2.18 \text{ in.}$$



There's always a solution in steel

77

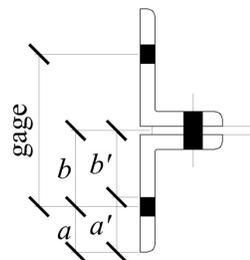
Example VB Corner Connection, I Gusset-to-Column (cont.)

**Gusset-to-Column – Prying of Column Flange
 (cont.):**

$$a = \min \{ (b_{fc} - \text{gage}) / 2, a \text{ from angle calcs} \} \\ = \min \{ (12 \text{ in.} - 5.5 \text{ in.}) / 2, 1.44 \text{ in.} \} \\ = 1.44 \text{ in.}$$

$$a' = a + d_b / 2 \leq 1.25b + d_b / 2 \\ = 1.44 \text{ in.} + 0.75 \text{ in.} / 2 \leq 1.25(2.56 \text{ in.}) + \\ 0.75 \text{ in.} / 2 \\ = 1.82 \text{ in.} < 3.58 \text{ in.} \text{ Use } 1.82 \text{ in.}$$

$$\rho = b' / a' = 2.18 \text{ in.} / 1.82 \text{ in.} = 1.20$$



There's always a solution in steel

78

Example VB Corner Connection, I Gusset-to-Column (cont.)

**Gusset-to-Column – Prying of Column Flange
 (cont.):**

$$p = p_{eff} = 5.88 \text{ in.}$$

$$\delta = 1 - d'/p = 1 - 0.8125 \text{ in.}/5.88 \text{ in.}$$

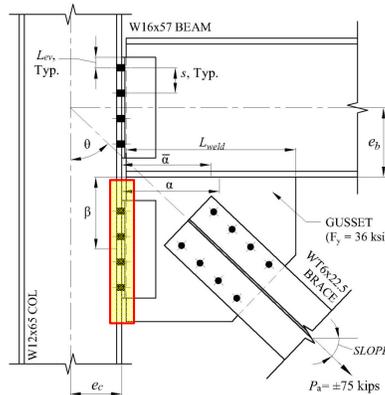
$$= 0.862$$

$$t_c = \sqrt{\frac{\Omega 4 B b'}{p F_u}} \quad (\text{AISC Manual Eq. 9-30a})$$

$$= \sqrt{\frac{1.67(4)(19.9 \text{ kips})(2.18 \text{ in.})}{(5.88 \text{ in.})(65 \text{ ksi})}}$$

$$= 0.871 \text{ in.} > t_{fc} = 0.605 \text{ in.}$$

→ check available strength of bolt including the effects of prying action



There's always a solution in steel

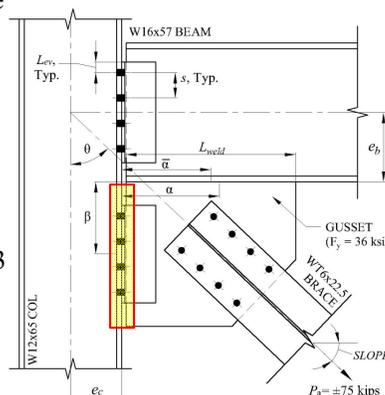
Example VB Corner Connection, I Gusset-to-Column (cont.)

**Gusset-to-Column – Prying of Column Flange
 (cont.):**

$$\alpha' = \frac{1}{\delta(1+\rho)} \left[\left(\frac{t_c}{t} \right)^2 - 1 \right] \quad (\text{AISC Manual Eq. 9-35})$$

$$= \frac{1}{0.862(1+1.20)} \left[\left(\frac{0.871 \text{ in.}}{0.605 \text{ in.}} \right)^2 - 1 \right]$$

$$= 0.565 > 0 \text{ and } < 1.0 \rightarrow \text{Manual Eq. 9-33 applies}$$



There's always a solution in steel

Example VB Corner Connection, I Gusset-to-Column (cont.)

**Gusset-to-Column – Prying of Column Flange
 (cont.):**

$$Q = \left(\frac{t}{t_c} \right)^2 (1 + \delta\alpha')$$

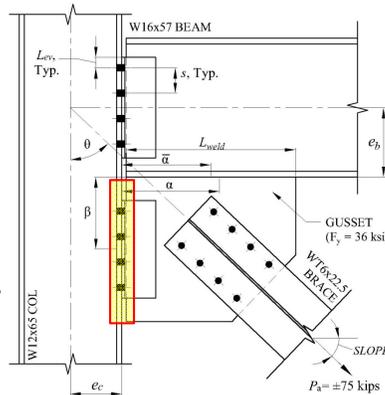
$$= \left(\frac{0.605 \text{ in.}}{0.871 \text{ in.}} \right)^2 [1 + (0.862)(0.565)]$$

$$= 0.717$$

The available strength of bolt including prying is

$$T_{avail} = BQ = (19.9 \text{ kips})(0.717)$$

$$= 14.3 \text{ kips} > T_{bolt} = 2.35 \text{ kips o.k.}$$



There's always a solution in steel

Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Bolt Bearing:

AISC Specification Eq. J3-6a

AISC Bolt Shear:

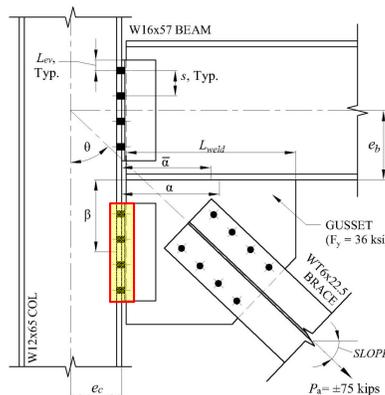
$$r_v/\Omega = 11.9 \text{ kips}$$

Column Bolt Bearing:

$$R_{brg(col)}/\Omega = 2.4d_b t F_u/\Omega$$

$$= 2.4(0.75 \text{ in.})(0.605 \text{ in.})(65 \text{ ksi})/2$$

$$= 35.4 \text{ kips}$$



There's always a solution in steel

The lecture will skip
 to slide 87.

Example VB Corner Connection, I Gusset-to-Column (cont.)

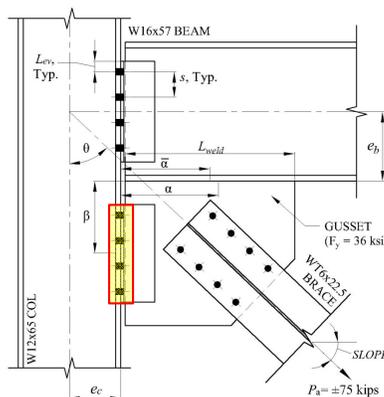
Gusset-to-Column – Bolt Bearing (cont.):

Column Bolt Tear Out (Center):

$$\begin{aligned}
 R_{tear(col_C)}/\Omega &= 1.2(s - d_{h_w})t_f F_u / \Omega \\
 &= 1.2(3 \text{ in.} - 13/16 \text{ in.}) \\
 &\quad \times (0.605 \text{ in.})(65 \text{ ksi})/2 \\
 &= 51.6 \text{ kips}
 \end{aligned}$$

Angle Bolt Bearing:

$$\begin{aligned}
 R_{brg(L)}/\Omega &= 2.4d_b t_a F_u / \Omega \\
 &= 2.4(0.75 \text{ in.})(0.375 \text{ in.})(58 \text{ ksi})/2 \\
 &= 19.6 \text{ kips}
 \end{aligned}$$



There's always a solution in steel

83

Example VB Corner Connection, I Gusset-to-Column (cont.)

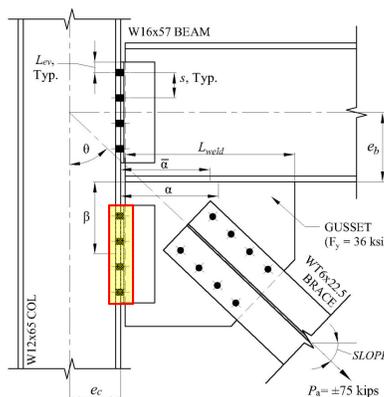
Gusset-to-Column – Bolt Bearing (cont.):

Angle Bolt Tear Out (Edge):

$$\begin{aligned}
 R_{tear(L_E)}/\Omega &= 1.2(L_{ev} - d_{h_w}/2)t_a F_u / \Omega \\
 &= 1.2(1.25 \text{ in.} - 13/16 \text{ in.}/2) \\
 &\quad \times (0.375 \text{ in.})(58 \text{ ksi})/2 \\
 &= 11.0 \text{ kips}
 \end{aligned}$$

Angle Bolt Tear Out (Center):

$$\begin{aligned}
 R_{tear(L_C)}/\Omega &= 1.2(s - d_{h_w})t_a F_u / \Omega \\
 &= 1.2(3 \text{ in.} - 13/16 \text{ in.})(0.375 \text{ in.}) \\
 &\quad \times (58 \text{ ksi})/2 \\
 &= 28.6 \text{ kips}
 \end{aligned}$$



There's always a solution in steel

84

Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Bolt Bearing (cont.):

$$R_{n(top)}/\Omega = \min \{r_v/\Omega, R_{brg(col)}/\Omega, R_{tear(col_C)}/\Omega, R_{brg(L)}/\Omega, R_{tear(L_C)}/\Omega\}$$

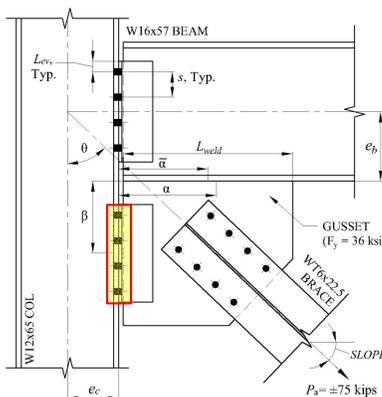
$$= \min \{11.9 \text{ kips}, 35.4 \text{ kips}, 51.6 \text{ kips}, 19.6 \text{ kips}, 28.6 \text{ kips}\}$$

$$= 11.9 \text{ kips}$$

$$R_{n(center)}/\Omega = \min \{r_v/\Omega, R_{brg(col)}/\Omega, R_{tear(col_C)}/\Omega, R_{brg(L)}/\Omega, R_{tear(L_C)}/\Omega\}$$

$$= \min \{11.9 \text{ kips}, 35.4 \text{ kips}, 51.6 \text{ kips}, 19.6 \text{ kips}, 28.6 \text{ kips}\}$$

$$= 11.9 \text{ kips}$$



There's always a solution in steel

85

Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Bolt Bearing (cont.):

$$R_{n(bot)}/\Omega = \min \{r_v/\Omega, R_{brg(col)}/\Omega, R_{tear(col_C)}/\Omega, R_{brg(L)}/\Omega, R_{tear(L_E)}/\Omega\}$$

$$= \min \{11.9 \text{ kips}, 35.4 \text{ kips}, 51.6 \text{ kips}, 19.6 \text{ kips}, 11.0 \text{ kips}\}$$

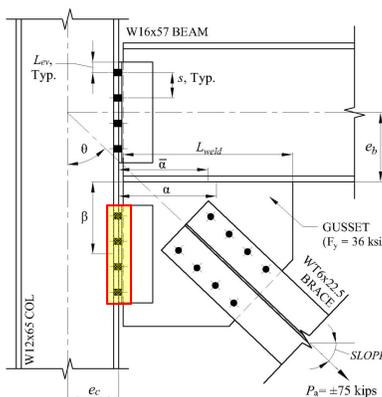
$$= 11.0 \text{ kips}$$

Total Bolt Strength

$$R_n/\Omega = [R_{n(top)}/\Omega + (R_{n(center)}/\Omega)(n - 2) + R_{n(bot)}/\Omega](2 \text{ lines})$$

$$= [11.9 \text{ kips} + (11.9 \text{ kips})(4 - 2) + 11.0 \text{ kips}](2)$$

$$= 93.4 \text{ kips} > V_c = 26.3 \text{ kips o.k.}$$



There's always a solution in steel

86

Example VB Corner Connection, I Gusset-to-Column (cont.)

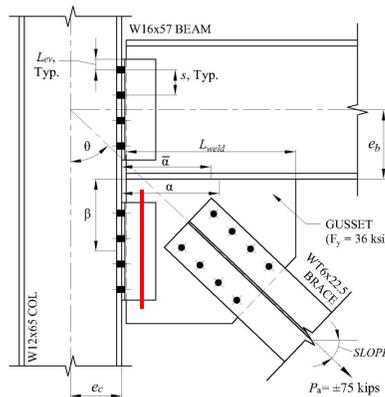
Gusset-to-Column – Angle Gross Shear:

AISC Specification Eq. J4-1

$$\frac{R_n}{\Omega} = \frac{0.6F_y A_g}{\Omega}$$

$$= \frac{0.6(36 \text{ ksi})(11.5 \text{ in.})(0.375 \text{ in.})}{1.5}$$

$$= 124 \text{ kips} > V_c = 26.3 \text{ kips o.k.}$$



There's always a solution in steel

87

Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Angle Net Shear:

AISC Specification Eq. J4-4

$$L_{nv} = L_{eff} - n(d_{h,width} + 1/16 \text{ in.})$$

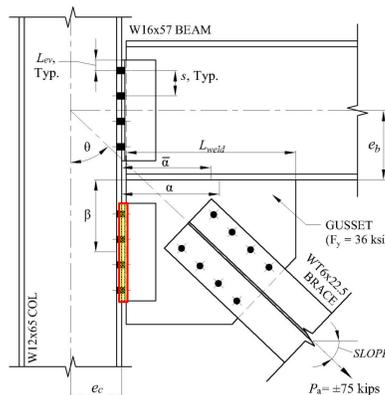
$$= 11.5 \text{ in.} - 4(13/16 \text{ in.} + 1/16 \text{ in.})$$

$$= 8 \text{ in.}$$

$$\frac{R_n}{\Omega} = \frac{0.6F_u A_{nv}}{\Omega}$$

$$= \frac{0.6(58 \text{ ksi})(2)(8 \text{ in.})(0.375 \text{ in.})}{2}$$

$$= 104 \text{ kips} > V_c = 26.3 \text{ kips o.k.}$$



There's always a solution in steel

88

Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Block Shear of Angles OSL:

AISC Spec Section J4.3 Block Shear Strength

$$\Omega = 2.00$$

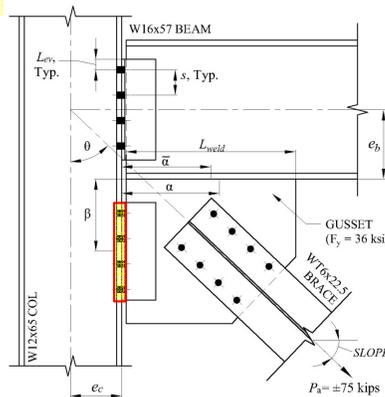
$$R_n = 0.6F_uA_{nv} + U_{bs}F_uA_{nt} \leq 0.6F_yA_{gv} + U_{bs}F_uA_{nt}$$

$$\text{Shear Rupture} = 0.6F_uA_{nv}$$

$$\text{Shear Yield} = 0.6F_yA_{gv}$$

$$\text{Tension Rupture} = F_uA_{nt}$$

$$U_{bs} = 1.0 \text{ for Direct Loaded Connections}$$



There's always a solution in steel

The lecture will skip
 to slide 94.

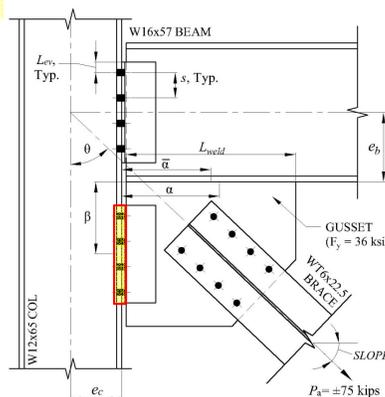
89

Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Block Shear of Angles OSL (cont.):

$$L_{gv} = L_{ev} + s(n - 1) = 1.25 \text{ in.} + (3 \text{ in.})(4 - 1) = 10.3 \text{ in.}$$

$$L_{nv} = L_{ev} + s(n - 1) - (n - 0.5)(d_h + 1/16 \text{ in.}) - (4 - 0.5)(7/8 \text{ in.}) = 7.19 \text{ in.}$$



There's always a solution in steel

90

Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Block Shear of Angles

OSL (cont.):

$$\begin{aligned}
 L_{gt} = L_{eh} &= a \text{ from prying calcs} \\
 &= [2(\text{angle OSL}) + t_p - \text{gage}]/2 \\
 &= [2(4 \text{ in.}) + 0.375 \text{ in.} - 5.5 \text{ in.}]/2 \\
 &= 1.44 \text{ in.}
 \end{aligned}$$

$$\begin{aligned}
 L_{nt} &= L_{eh} - 0.5(\text{hole length} + 1/16 \text{ in.}) \\
 &= 1.44 \text{ in.} - 0.5(1 + 1/16 \text{ in.}) \\
 &= 0.91 \text{ in.}
 \end{aligned}$$

AISC Specification TABLE J3.3
 Nominal Hole Dimensions, in.

Bolt Diameter, in.	Hole Dimensions			
	Standard (Dia.)	Oversize (Dia.)	Short-Slot (Width × Length)	Long-Slot (Width × Length)
1/2	9/16	5/8	9/16 × 1 1/16	9/16 × 1 1/4
5/8	1 1/16	13/16	1 1/16 × 7/8	1 1/16 × 1 9/16
3/4	13/16	15/16	1 3/16 × 1	1 3/16 × 1 7/8
7/8	15/16	1 1/8	1 5/16 × 1 1/8	1 5/16 × 2 1/8
1	1 7/16	1 1/4	1 7/16 × 1 9/16	1 7/16 × 2 1/2
≥ 1 1/8	d + 3/16	d + 9/16	(d + 7/16) × (d + 9/16)	(d + 7/16) × (2.5 × d)



There's always a solution in steel

91

Example VB Corner Connection, I Gusset-to-Column (cont.)

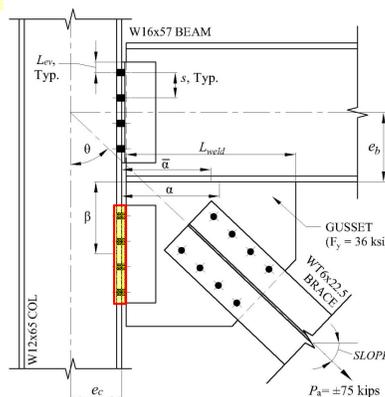
Gusset-to-Column – Block Shear of Angles

OSL (cont.):

$$\begin{aligned}
 A_{gv} &= 2L_{gv}t_a = 2(10.3 \text{ in.})(0.375 \text{ in.}) \\
 &= 7.73 \text{ in.}^2
 \end{aligned}$$

$$\begin{aligned}
 A_{nv} &= 2L_{nv}t_a = 2(7.19 \text{ in.})(0.375 \text{ in.}) \\
 &= 5.39 \text{ in.}^2
 \end{aligned}$$

$$\begin{aligned}
 A_{nt} &= 2L_{nt}t_a = 2(0.91 \text{ in.})(0.375 \text{ in.}) \\
 &= 0.68 \text{ in.}^2
 \end{aligned}$$



There's always a solution in steel

92

Example VB Corner Connection, I Brace-to-Gusset (cont.)

Gusset-to-Column – Block Shear of Angles

OSL (cont.):

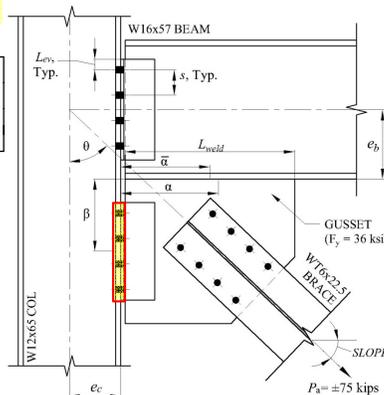
$$R_n = \min \left[\begin{aligned} &0.6(58 \text{ ksi})(5.39 \text{ in.}^2) = 187.57 \text{ kips} \\ &0.6(36 \text{ ksi})(7.73 \text{ in.}^2) = 166.97 \text{ kips} \end{aligned} \right]$$

$$+ [1(58 \text{ ksi})(0.68 \text{ in.}^2)]$$

$$= 166.97 \text{ kips} + 39.44 \text{ kips} = 206.41 \text{ kips}$$

$$R_n/\Omega = (206.41 \text{ kips})/2$$

$$= 103 \text{ kips} > V_c = 26.3 \text{ kips o.k.}$$



There's always a solution in steel

93

Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Block Shear of Gusset:

AISC Spec Section J4.3 Block Shear Strength

$$\Omega = 2.00$$

$$R_n = 0.6F_u A_{nv} + U_{bs} F_u A_{nt}$$

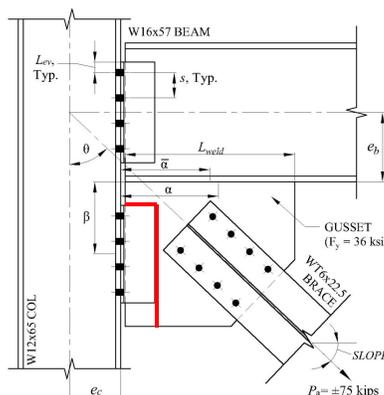
$$\leq 0.6F_y A_{gv} + U_{bs} F_u A_{nt}$$

$$\text{Shear Rupture} = 0.6F_u A_{nv}$$

$$\text{Shear Yield} = 0.6F_y A_{gv}$$

$$\text{Tension Rupture} = F_u A_{nt}$$

$$U_{bs} = 1.0 \text{ for Direct Loaded Connections}$$



There's always a solution in steel

94

Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Block Shear of Gusset:

Gusset is welded

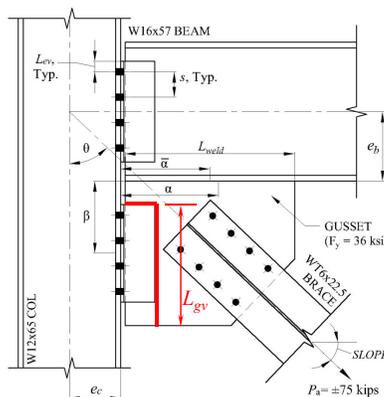
For Shear check:

$$L_{gv} = 14.25 \text{ in. (from geometric layout)}$$

$$L_{gt} = k = 3.5 \text{ in.}$$

$$L_{nv} = 14.25 \text{ in.}$$

$$L_{nt} = k = 3.5 \text{ in.}$$



There's always a solution in steel

95

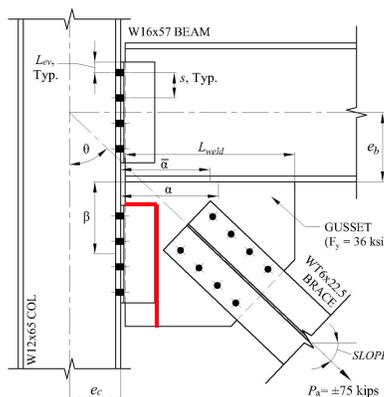
Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Block Shear of Gusset (cont.):

$$A_{gv} = L_{gv}t_p = (14.25 \text{ in.})(0.375 \text{ in.}) = 5.34 \text{ in.}^2$$

$$A_{nv} = L_{nv}t_p = (14.25 \text{ in.})(0.375 \text{ in.}) = 5.34 \text{ in.}^2$$

$$A_{nt} = L_{nt}t_p = (3.5 \text{ in.})(0.375 \text{ in.}) = 1.31 \text{ in.}^2$$



There's always a solution in steel

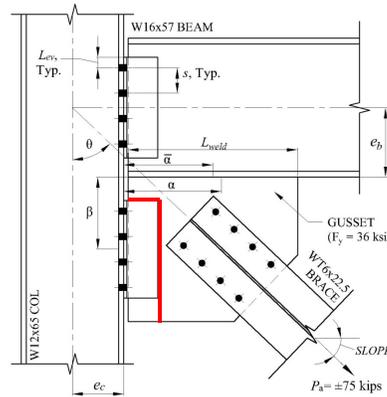
96

Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Block Shear of Gusset (cont.):

$$R_n = \min \left[\begin{array}{l} 0.6(58 \text{ ksi})(5.34 \text{ in.}^2) = 185.83 \text{ kips} \\ 0.6(36 \text{ ksi})(5.34 \text{ in.}^2) = 115.34 \text{ kips} \end{array} \right] \\
 + [1(58 \text{ ksi})(1.31 \text{ in.}^2)] \\
 = 115.34 \text{ kips} + 75.98 \text{ kips} = 191.32 \text{ kips}$$

$$R_n/\Omega = (191.32 \text{ kips})/2 \\
 = 96 \text{ kips} > V_c = 26.3 \text{ kips o.k.}$$



There's always a solution in steel

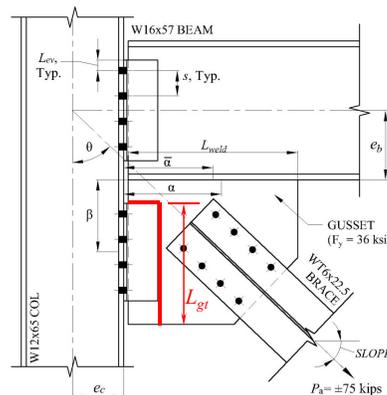
Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Block Shear of Gusset (cont.):

Gusset is welded

For Axial check:

$$L_{gv} = k = 3.5 \text{ in.} \\
 L_{gt} = 14.25 \text{ in. (from geometric layout)} \\
 L_{nv} = k = 3.5 \text{ in.} \\
 L_{nt} = 14.25 \text{ in.}$$



There's always a solution in steel

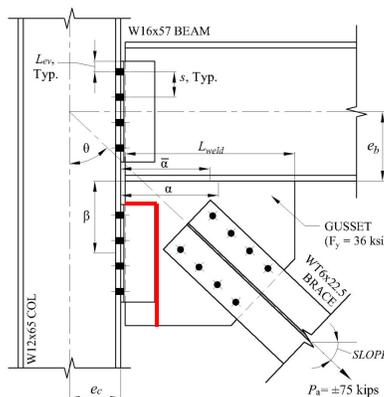
Example VB Corner Connection, I Gusset-to-Column (cont.)

**Gusset-to-Column – Block Shear of Gusset
 (cont.):**

$$A_{gv} = L_{gv}t_p = (3.5 \text{ in.})(0.375 \text{ in.}) = 1.31 \text{ in.}^2$$

$$A_{nv} = L_{nv}t_p = (3.5 \text{ in.})(0.375 \text{ in.}) = 1.31 \text{ in.}^2$$

$$A_{nt} = L_{nt}t_p = (14.25 \text{ in.})(0.375 \text{ in.}) = 5.34 \text{ in.}^2$$



There's always a solution in steel

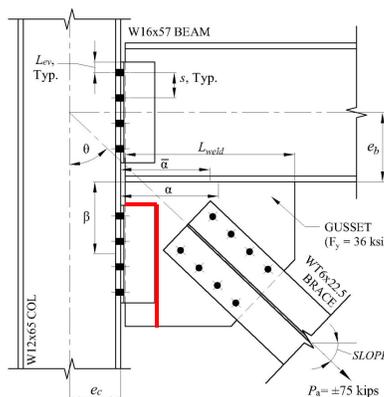
Example VB Corner Connection, I Gusset-to-Column (cont.)

**Gusset-to-Column – Block Shear of Gusset
 (cont.):**

$$R_n = \min \left[\begin{array}{l} 0.6(58 \text{ ksi})(1.31 \text{ in.}^2) = 45.59 \text{ kips} \\ 0.6(36 \text{ ksi})(1.31 \text{ in.}^2) = 28.30 \text{ kips} \end{array} \right] + [1(58 \text{ ksi})(5.34 \text{ in.}^2)]$$

$$= 28.30 \text{ kips} + 309.72 \text{ kips} = 338.02 \text{ kips}$$

$$R_n/\Omega = (338.02 \text{ kips})/2 = 169 \text{ kips} > H_c = 18.8 \text{ kips} \text{ o.k.}$$



There's always a solution in steel

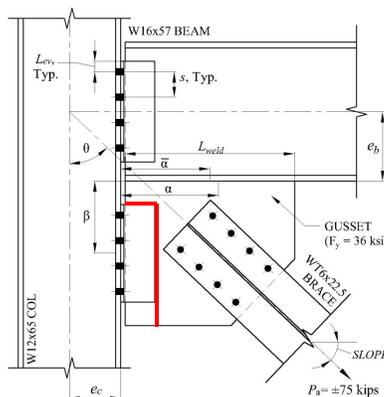
Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Block Shear of Gusset (cont.):

Unity Check (Sum of Squares):

$$\left(\frac{V_c}{R_{nv}/\Omega}\right)^2 + \left(\frac{H_c}{R_{nt}/\Omega}\right)^2 \leq 1.0$$

$$\left(\frac{26.3 \text{ kips}}{96 \text{ kips}}\right)^2 + \left(\frac{18.8 \text{ kips}}{169 \text{ kips}}\right)^2 = 0.09 < 1.0 \quad \text{o.k.}$$



There's always a solution in steel

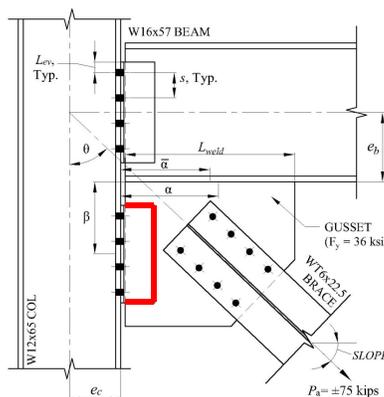
Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Size Weld:

$$\begin{aligned} P_c &= \sqrt{(H_c)^2 + (V_c)^2} \\ &= \sqrt{(18.8 \text{ kips})^2 + (26.3 \text{ kips})^2} \\ &= 32.3 \text{ kips} \end{aligned}$$

$$\begin{aligned} \theta &= \tan^{-1}(H_c/V_c) = \tan^{-1}(18.8 \text{ kips}/26.3 \text{ kips}) \\ &= 35.6^\circ \end{aligned}$$

$$\begin{aligned} l &= s(n-1) + 2L_{ey} \\ &= (3 \text{ in.})(4-1) + 2(1.25 \text{ in.}) \\ &= 11.5 \text{ in.} \end{aligned}$$



There's always a solution in steel

Example VB Corner Connection, I Gusset-to-Column (cont.)

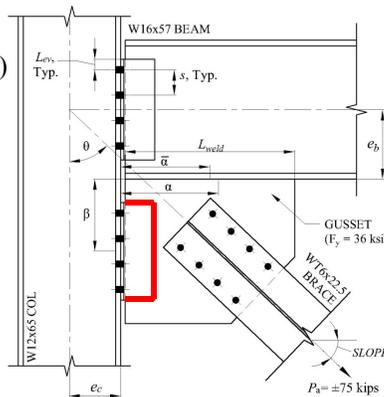
Gusset-to-Column – Size Weld (cont.):

$$\begin{aligned}
 D_{min} &= P_c \Omega / (2CC_1 L) \\
 &= 32.3 \text{ kips}(2) / ((2)(2.96)(1.0)(11.5 \text{ in.})) \\
 &= 0.949 < 4 \text{ (16}^{\text{th}} \text{ of an inch)} \\
 &\quad \frac{1}{4}'' \text{ fillet weld o.k.}
 \end{aligned}$$

$$\begin{aligned}
 t_{min} &= 2(0.928 D_{min}) / [0.6(F_u / \Omega)] \\
 &= 2(0.928)(0.949) / [0.6(58 \text{ ksi} / 2)] \\
 &= 0.101 \text{ in.} > t_p = 0.375 \text{ in. o.k.}
 \end{aligned}$$

Note, the above is same as *Manual* Eq 9-3:

$$t_{min} = 6.19 D / F_u$$



There's always a solution in steel

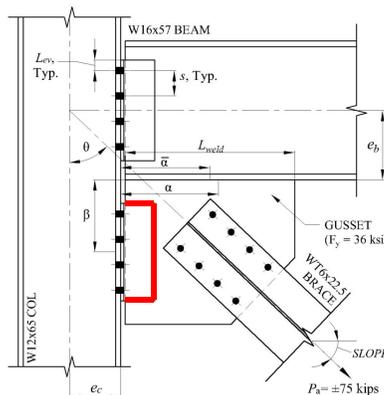
105

Example VB Corner Connection, I Gusset-to-Column (cont.)

Gusset-to-Column – Size Weld (cont.):

If $t_{min} < t_p$, no reduction necessary.

$$\text{If } t_{min} > t_p, \frac{R_w}{\Omega} = \left(\frac{R_n}{\Omega} \right) \left(\frac{t_p}{t_{min}} \right)$$



There's always a solution in steel

106

Example VB Corner Connection, I Gusset-to-Beam



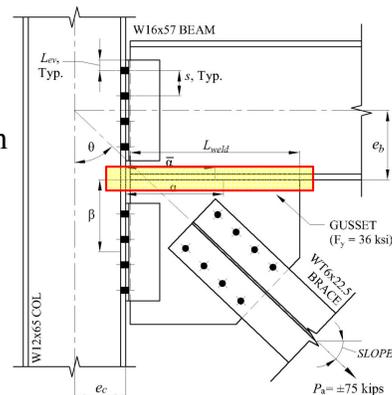
There's always a solution in steel

107

Example VB Corner Connection, I Gusset-to-Beam

The gusset-to-beam will be designed by doing the following:

- Size weld between gusset and beam
- Check gusset for shear and tension at weld line
- Check beam web yielding
- Check local beam web crippling



There's always a solution in steel

108

Design of Fillet Welds

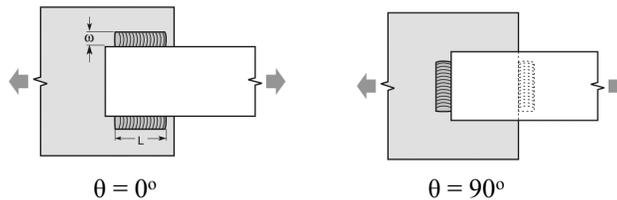
Section J2.4(a) allows the directional strength increase for linear weld groups.

$$R_n = 0.6F_{EXX}(1.0 + 0.5 \sin^{1.5} \theta)A_w$$

F_w = nominal unit stress, ksi

F_{EXX} = electrode classification number, i.e., minimum specified tensile strength, ksi

θ = angle of loading measured from the weld longitudinal axis, degrees



There's always a solution in steel

109

Design of Fillet Welds

Again this is more commonly written:

For ASD: $R_n / \Omega = 0.928(1.0 + 0.5 \sin^{1.5} \theta)DL$

For LRFD: $\phi R_n = 1.392(1.0 + 0.5 \sin^{1.5} \theta)DL$



There's always a solution in steel

110

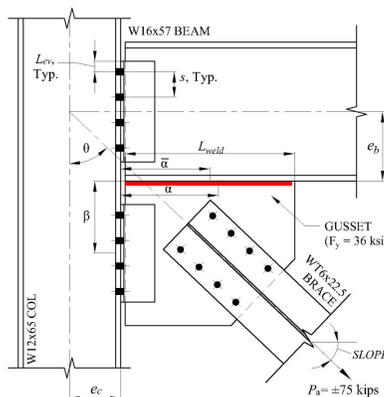
Example VB Corner Connection, I Gusset-to-Beam (cont.)

Gusset-to-Beam – Size Weld:

$$f_x = H_b/L_{weld} = 35.6 \text{ kips}/20 \text{ in.} \\ = 1.78 \text{ kips/in.}$$

$$f_y = V_b/L_{weld} = 25.4 \text{ kips}/20 \text{ in.} \\ = 1.27 \text{ kips/in.}$$

$$f_y = 4M_b/L_{weld}^2 \\ = 4(25.4 \text{ kip-in.})/(20 \text{ in.})^2 \\ = 0.254 \text{ kips/in.}$$



There's always a solution in steel

111

Example VB Corner Connection, I Gusset-to-Beam (cont.)

Gusset-to-Beam – Size Weld (cont.):

$$f_{peak} = \sqrt{(f_x)^2 + (f_y + f'_y)^2} \\ = \sqrt{(1.78 \text{ k/in.})^2 + (1.27 \text{ k/in.} + 0.254 \text{ k/in.})^2} \\ = 2.34 \text{ kips/in.}$$

$$1.25 f_{avg} = (1.25) \left(\frac{1}{2} \right) \left[\sqrt{(f_x)^2 + (f_y + f'_y)^2} + \sqrt{(f_x)^2 + (f_y - f'_y)^2} \right] \\ = (1.25) \left(\frac{1}{2} \right) \left[\sqrt{(1.78 \text{ k/in.})^2 + (1.27 \text{ k/in.} + 0.254 \text{ k/in.})^2} \right. \\ \left. + \sqrt{(1.78 \text{ k/in.})^2 + (1.27 \text{ k/in.} - 0.254 \text{ k/in.})^2} \right] \\ = 2.75 \text{ kips/in.}$$



There's always a solution in steel

112

Example VB Corner Connection, I Gusset-to-Beam (cont.)

Gusset-to-Beam – Size Weld (cont.):

$$\begin{aligned}\theta &= \tan^{-1} [(f_y + f_y)/f_x] \\ &= \tan^{-1} [(1.27 \text{ kips/in.} + 0.254 \text{ kips/in.})/1.78 \text{ kips/in.}] \\ &= 40.6^\circ\end{aligned}$$

$$\begin{aligned}f_w &= 0.60(F_{EXX}/\Omega)(0.707D/16)(1.0 + 0.50 \sin^{1.5} \theta) \\ &= 0.928D (1.0 + 0.50 \sin^{1.5} 40.6^\circ) \\ &= 0.928D(1.26)\end{aligned}$$



There's always a solution in steel

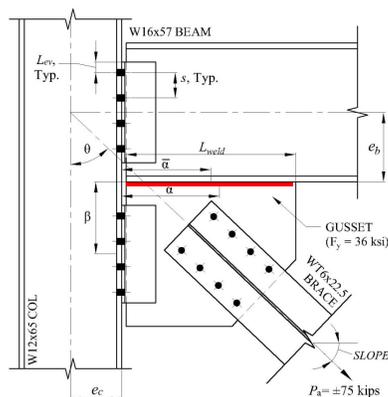
113

Example VB Corner Connection, I Gusset-to-Beam (cont.)

Gusset-to-Beam – Size Weld (cont.):

$$\begin{aligned}D_{min} &= \max(f_{peak}, 1.25f_{avg}) / [f_w (2 \text{ sides})] \\ &= \max(2.34 \text{ kips/in.}, 2.75 \text{ kips/in.}) / \\ &\quad [0.928(1.26)(2)] \\ &= 1.18 > 4 \text{ (16}^{\text{th}} \text{ on an inch) o.k.} \\ &\quad \text{(1/4" fillet provided)}\end{aligned}$$

Also, per AISC *Specification* Table 2.4,
 minimum size fillet weld for 3/8" gusset =
 3/16" < 1/4" **o.k.**



There's always a solution in steel

114

Example VB Corner Connection, I Gusset-to-Beam (cont.)

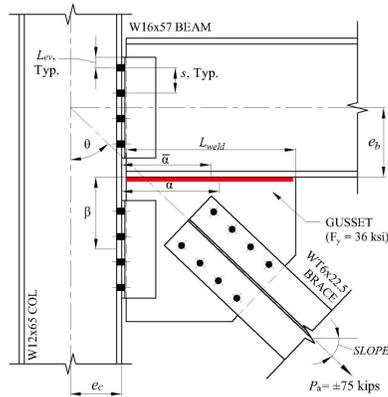
Gusset-to-Beam – Check Gusset:

Shear:

$$\begin{aligned} t_{min(gusset)} &= f_x/[0.6(F_y/\Omega)] \\ &= (1.78 \text{ kips/in.})/[0.6(36 \text{ ksi}/1.5)] \\ &= 0.124 \text{ in.} < t_p = 0.375 \text{ in. o.k.} \end{aligned}$$

Tension:

$$\begin{aligned} t_{min(gusset)} &= (f_y + f_x)/(F_y/\Omega) \\ &= (1.27 \text{ k/in.} + 0.254 \text{ k/in.}) / \\ &\hspace{10em} (36 \text{ ksi}/1.67) \\ &= 0.071 \text{ in.} < t_p = 0.375 \text{ in. o.k.} \end{aligned}$$



There's always a solution in steel

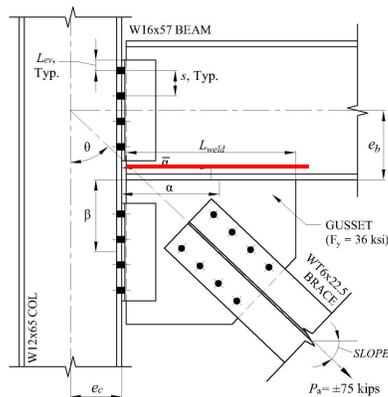
115

Example VB Corner Connection, I Gusset-to-Beam (cont.)

Gusset-to-Beam – Beam Web Yielding:

$$\begin{aligned} P_{equival} &= 2[M_b/(L_{weld}/2)] + V_b \\ &= 2[25.4 \text{ k-in.}/(20 \text{ in.}/2)] + 25.4 \text{ kips} \\ &= 30.5 \text{ kips for full weld length} \end{aligned}$$

$$\begin{aligned} R_n/\Omega &= t_w(L_{weld} + 2.5k)(F_y/\Omega) \\ &= (0.43 \text{ in.})[20 \text{ in.} + 2.5(1.12 \text{ in.})] \\ &\hspace{10em} \times (50 \text{ ksi}/1.5) \\ &= 327 \text{ kips} > 30.5 \text{ kips o.k.} \end{aligned}$$



There's always a solution in steel

116

Example VB Corner Connection, I Gusset-to-Beam (cont.)

Gusset-to-Beam – Local Beam Web Crippling:

$P_{equival} = 30.5$ kips for full weld length (from beam web yielding calcs)

$$\frac{R_n}{\Omega} = \frac{0.8t_w^2 \left[1 + 3 \left(\frac{L_{weld}}{d} \right) \left(\frac{t_w}{t_f} \right)^{1.5} \right] \sqrt{\frac{E F_{yw} t_f}{t_w}}}{\Omega}$$

$$= \frac{\left[\frac{0.8(0.43 \text{ in.})^2}{2} \left[1 + 3 \left(\frac{20 \text{ in.}}{16.4 \text{ in.}} \right) \left(\frac{0.43 \text{ in.}}{0.715 \text{ in.}} \right)^{1.5} \right] \right] \times \sqrt{\frac{(29,000 \text{ ksi})(50 \text{ ksi})(0.715 \text{ in.})}{0.43 \text{ in.}}}}{2} = 311 \text{ kips} > 30.5 \text{ kips o.k.}$$



There's always a solution in steel

117

Example VB Corner Connection, I Beam-to-Column



There's always a solution in steel

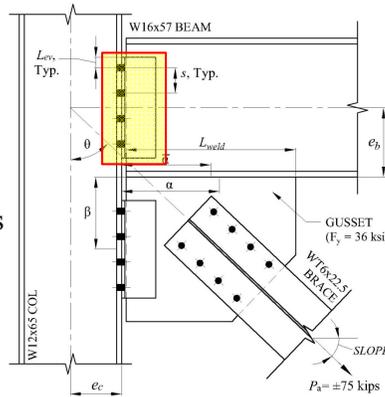
118



Example VB Corner Connection, I Beam-to-Column

Finally, the beam-to-column will be designed, checking the beam end as a shear and axially loaded end connection.

- a. Check bolts at column flange
- b. Check prying of angles and column flanges
- c. Check bolt bearing and tearout of angles and column flange
- d. Check gross and net section shear and block shear for angles
- e. Check block shear of beam
- f. Check angle welds



There's always a solution in steel

Example VB Corner Connection, I Beam-to-Column (cont.)

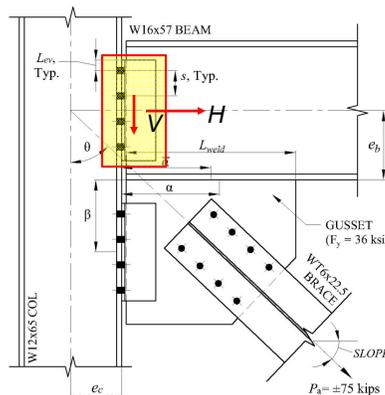
Beam-to-Column – Forces:

$V_{b(top)} = 0$ kips (no upper brace)

$V_{b(bot)} = 25.4$ kips (from lower brace)

$PTF =$ Transfer force from adjacent beam into the braced bay
 $= 0$ kips (no transfer force)

$V_g = 41.9$ kips (50% UDL for span of 25 ft)
 (UDL projects: not preferred)



There's always a solution in steel

Example VB Corner Connection, I Beam-to-Column (cont.)



Table 3-6 (continued)
**Maximum Total
 Uniform Load, kips**
 W-Shapes

$F_y = 50$ ksi

Shape	W16x									
	89		77		67		57		50	
	ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD	ASD	LRFD
7							282	423	248	372
8							262	394	230	345
9	353	529	300	450			233	350	204	307
10	349	525	299	450	258	386	210	315	184	276
11	318	477	272	409	236	355	191	286	167	251
12	291	438	250	375	216	325	175	263	153	230
13	269	404	230	346	200	300	161	242	141	212
14	250	375	214	321	185	279	150	225	131	197
15	233	350	200	300	173	260	140	210	122	184
16	218	328	187	281	162	244	131	197	115	173
17	205	309	176	265	153	229	123	185	108	162
18	194	292	166	250	144	217	116	175	102	153
19	184	276	158	237	137	205	110	166	96.6	145
20	175	263	150	225	130	195	105	158	91.8	138
21	166	250	143	214	124	186	99.8	150	87.4	131
22	159	239	136	205	118	177	95.3	143	83.5	125
23	152	228	130	196	113	170	91.1	137	79.8	120
24	146	219	125	188	108	163	87.3	131	76.5	115
25	140	210	120	180	104	156	83.8	126	73.5	110
26	134	202	115	173	99.8	150	80.6	121	70.6	106

50% UDL
 = 0.5 (83.8)
 = 41.9 kips



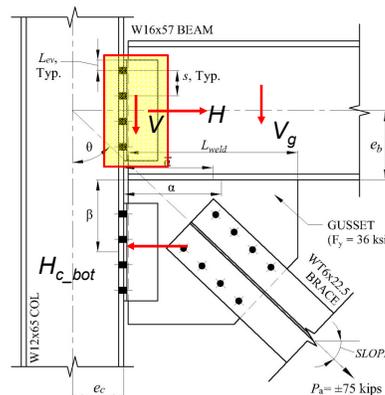
121

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Forces (cont.):

$$\begin{aligned}
 V &= V_g + V_{b(top)} + V_{b(bot)} \\
 &= 41.9 \text{ kips} + 0 \text{ kips} + 25.4 \text{ kips} \\
 &= 67.3 \text{ kips}
 \end{aligned}$$

$$\begin{aligned}
 H &= \max(H_{c(bot)}, H_{c(top)} + PTF) \\
 &= \max(18.8 \text{ kips}, 0 \text{ kips} + 0 \text{ kips}) \\
 &= 18.8 \text{ kips}
 \end{aligned}$$



There's always a solution in steel

122

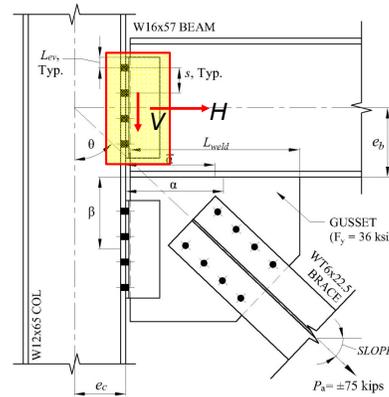


Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Forces (cont.):

Notes:

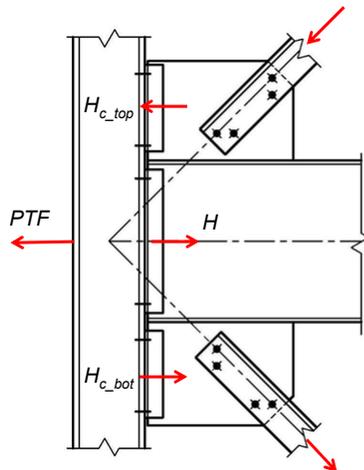
1. Distortional forces not considered
2. Could use $H = H_{c(bot)} - (H_{c(top)} + PTF)$ if checking exact load case
3. Add opposite H_c if braces are both in compression.
4. Conservatively, the maximum V will be checked with H . However, when the bottom brace is in compression, H is a tension force at the beam and V_b would reduce V_g .



There's always a solution in steel

123

VB Corner Connection

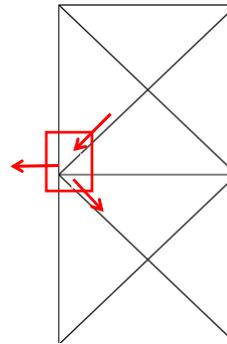


If exact load case not known:

$$H = \max(H_{c(bot)}, H_{c(top)} + PTF)$$

If exact load case is known:

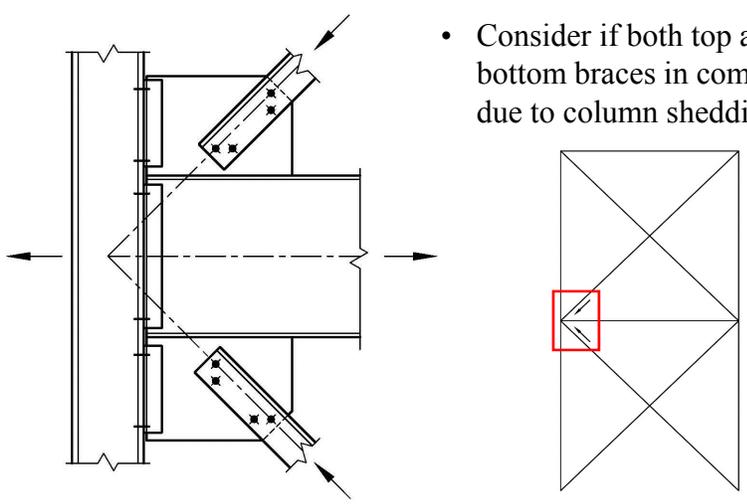
$$H = H_{c(bot)} - (H_{c(top)} + PTF)$$



There's always a solution in steel

124

VB Corner Connection



- Consider if both top and bottom braces in compression due to column shedding

 There's always a solution in steel

125

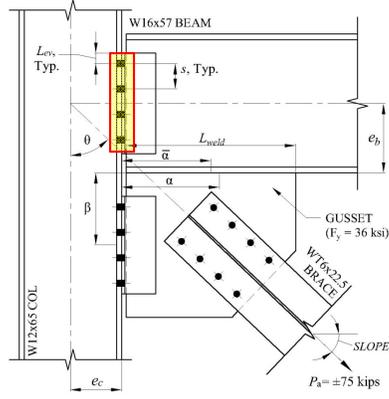
Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Bolts:

$$\begin{aligned}
 R_b/\Omega &= 2n(r_v/\Omega) \\
 &= 2(4)(11.9 \text{ kips}) \\
 &= 95.2 \text{ kips} > V = 67.3 \text{ kips} \text{ o.k.}
 \end{aligned}$$

Check Shear and Tension:

$$\begin{aligned}
 V_{bolt} &= V_c/(2n) = 67.3 \text{ kips}/[(2)(4)] \\
 &= 8.41 \text{ kips}
 \end{aligned}$$

$$\begin{aligned}
 T_{bolt} &= H_c/(2n) = 18.8 \text{ kips}/[(2)(4)] \\
 &= 2.35 \text{ kips}
 \end{aligned}$$


 There's always a solution in steel

The lecture will skip to slide 159. 126

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Bolts (cont.):

Check Shear and Tension (cont.):

$$A_b = \frac{\pi d_b^2}{4}$$

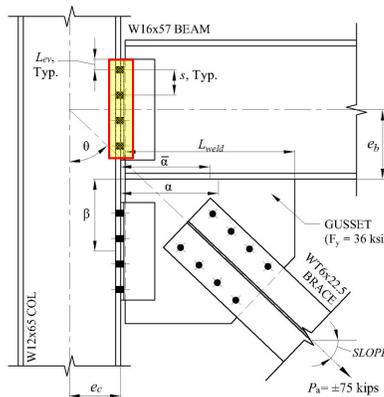
$$= \frac{3.14(0.75 \text{ in.})^2}{4}$$

$$= 0.442 \text{ in.}^2$$

$$f_v = V_{bolt}/A_b$$

$$= 8.41 \text{ kips}/0.442 \text{ in.}^2$$

$$= 19.0 \text{ ksi}$$



There's always a solution in steel

127

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Bolts (cont.):

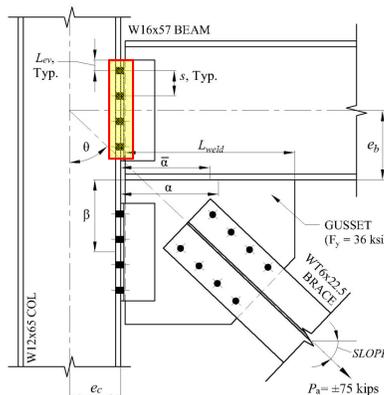
Check Shear and Tension (cont.):

$$F'_{nt} = 1.3F_{nt} - \Omega F_{nv} f_{rv}/F_{nv} \leq F_{nt} \quad (\text{Spec J3-3a})$$

$$= 1.3(90 \text{ ksi}) - 2(90 \text{ ksi})(19.0 \text{ ksi})/(54 \text{ ksi})$$

$$= 53.7 \text{ ksi} < 90 \text{ ksi, use } 53.7 \text{ ksi}$$

AISC Specification TABLE J3.2 Nominal Strength of Fasteners and Threaded Parts, ksi (MPa)		
Description of Fasteners	Nominal Tensile Strength, F_{nt} , ksi (MPa) ^[1]	Nominal Shear Strength in Bearing-Type Connections, F_{nv} , ksi (MPa) ^[2]
A307 bolts	45 (310)	27 (188) ^{[1][6]}
Group A (e.g., A325) bolts, when threads are not excluded from shear planes	90 (620)	54 (372)



There's always a solution in steel

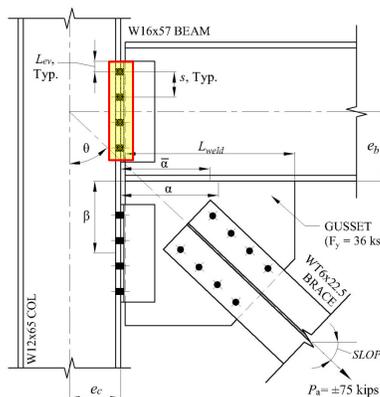
128

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Bolts (cont.):

Check Shear and Tension (cont.):

$$\begin{aligned} \frac{r_t}{\Omega} &= \frac{F'_{nt} A_b}{\Omega} \quad (\text{AISC Spec J3-2}) \\ &= \frac{(53.7 \text{ ksi})(0.442 \text{ in.}^2)}{2} \\ &= 11.9 \text{ kips} > T_{bolt} = 2.35 \text{ kips o.k.} \end{aligned}$$



There's always a solution in steel

129

Example VB Corner Connection, I Beam-to-Column (cont.)

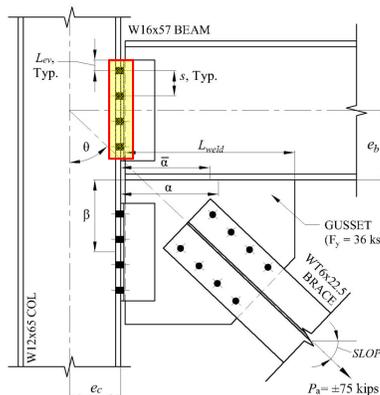
Beam-to-Column – Prying of Angles :

For connections to column webs, there is no tension force on the angle due to the brace forces since $H_c = 0$ kips. For this example, which is to a column flange:

$$T_{bolt} = H/(2n) = 18.8 \text{ kips}/[(2)(4)] = 2.35 \text{ kips}$$

$$\begin{aligned} b &= \text{gage}/2 - t_w/2 - t_a/2 \\ &= 5.5 \text{ in.}/2 - 0.43 \text{ in.}/2 - 0.375/2 = 2.35 \text{ in.} \end{aligned}$$

$$\begin{aligned} b' &= b - d_b/2 = \\ &= 2.35 \text{ in.} - 0.75 \text{ in.}/2 = 1.97 \text{ in.} \end{aligned}$$



There's always a solution in steel

130

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Prying of Angles (cont.):

$$a = [2(\text{angle OSL}) + t_w - \text{gage}] / 2$$

$$= [2(4 \text{ in.}) + 0.43 \text{ in.} - 5.5 \text{ in.}] / 2$$

$$= 1.47 \text{ in.}$$

$$a' = a + d_b / 2 \leq 1.25b + d_b / 2$$

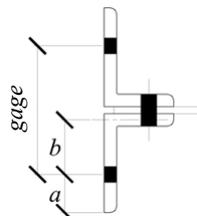
$$= 1.47 \text{ in.} + 0.75 \text{ in.} / 2$$

$$\leq 1.25(2.35 \text{ in.}) + 0.75 \text{ in.} / 2$$

$$= 1.85 \text{ in.} \leq 3.31 \text{ in.}$$

$$= 1.85 \text{ in.}$$

$$\rho = b' / a' = 1.97 \text{ in.} / 1.85 \text{ in.} = 1.06$$



There's always a solution in steel

131

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Prying of Angles (cont.):

$$p = L/n = 11.5 \text{ in.} / 4$$

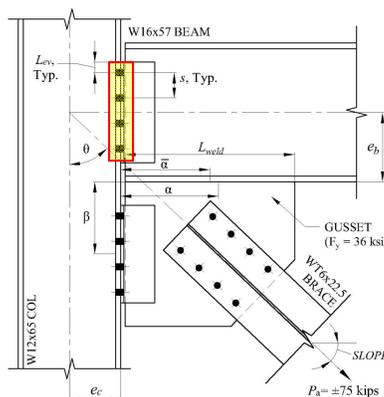
$$= 2.88 \text{ in. (tributary area per bolt)}$$

$$\delta = 1 - d'/p = 1 - 0.8125 \text{ in.} / 2.88 \text{ in.}$$

$$= 0.717$$

$$B = r_t / \Omega = 11.9 \text{ kips}$$

(bolt available tensile strength from previously)



There's always a solution in steel

132

Example VB Corner Connection, I Beam-to-Column (cont.)

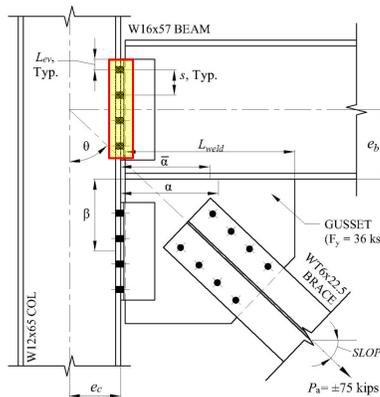
Beam-to-Column – Prying of Angles (cont.):

$$t_c = \sqrt{\frac{\Omega 4 B b'}{p F_u}} \quad (\text{AISC Manual Eq. 9-30a})$$

$$= \sqrt{\frac{1.67(4)(11.9 \text{ kips})(1.97 \text{ in.})}{(2.88 \text{ in.})(58 \text{ ksi})}}$$

$$= 0.968 \text{ in.}$$

t_c = minimum thickness of angles to develop full available tensile strength of bolt with no prying



There's always a solution in steel

133

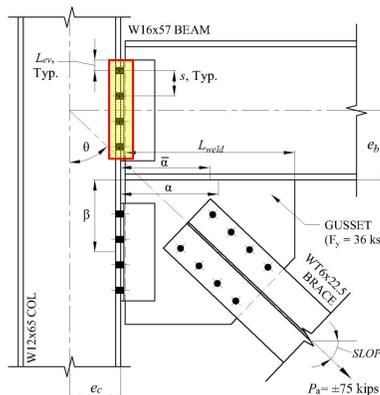
Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Prying of Angles (cont.):

$$\alpha' = \frac{1}{\delta(1+\rho)} \left[\left(\frac{t_c}{t} \right)^2 - 1 \right] \quad (\text{AISC Manual Eq. 9-35})$$

$$= \frac{1}{0.717(1+1.06)} \left[\left(\frac{0.968 \text{ in.}}{0.375 \text{ in.}} \right)^2 - 1 \right]$$

$$= 3.83 \text{ in.}$$



There's always a solution in steel

134

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Prying of Angles (cont.):

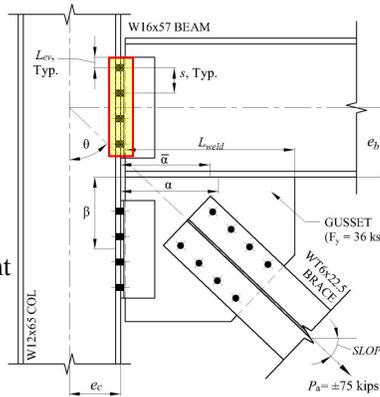
Note:

When $\alpha' < 0$, this means that the fitting has sufficient strength and stiffness to develop the full bolt available tensile strength,

$$Q = 1 \quad (\text{AISC Manual Eq. 9-32})$$

When $0 \leq \alpha' < 1$, this means that the fitting has sufficient strength and stiffness to develop the full bolt available tensile strength, but insufficient stiffness to prevent prying action,

$$Q = \left(\frac{t}{t_c} \right)^2 (1 + \delta \alpha') \quad (\text{AISC Manual Eq. 9-33})$$



There's always a solution in steel

135

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Prying of Angles (cont.):

For the example,

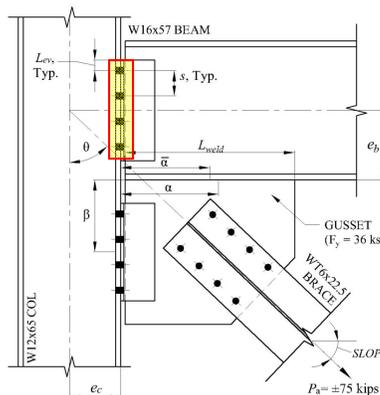
$$\alpha' = 3.83 > 1$$

This means that the angle has insufficient strength to develop the full bolt available tensile strength. Therefore,

$$Q = \left(\frac{t}{t_c} \right)^2 (1 + \delta) \quad (\text{AISC Manual Eq. 9-34})$$

$$= \left(\frac{0.375 \text{ in.}}{0.968 \text{ in.}} \right)^2 (1 + 0.717 \text{ in.})$$

$$= 0.258$$



There's always a solution in steel

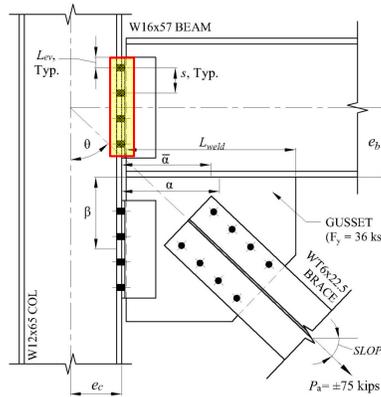
136

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Prying of Angles (cont.):

The available tensile strength including the effects of prying action, T_{avail} , is:

$$T_{avail} = BQ = (11.9 \text{ kips})(0.258) = 3.07 \text{ kips} > T_{bolt} = 2.35 \text{ kips o.k.}$$



There's always a solution in steel

137

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Prying of Angles (cont.):

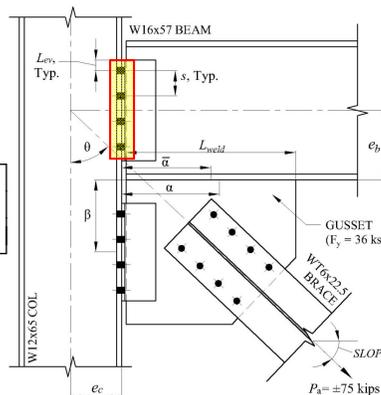
If prying force, q , needs to be determined:

$$\alpha = \left(\frac{1}{\delta} \right) \left[\frac{T}{B} \left(\frac{t_c}{t} \right)^2 - 1 \right] \quad (\text{AISC Manual Eq. 9-29})$$

$$= \left(\frac{1}{0.717} \right) \left[\left(\frac{2.35 \text{ kips}}{11.9 \text{ kips}} \right) \left(\frac{0.968 \text{ in.}}{0.375 \text{ in.}} \right)^2 - 1 \right]$$

$$= 0.441 > 0 \text{ and } < 1.0$$

Note: When $\alpha > 1$, the connection is not adequate.



There's always a solution in steel

138

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Prying of Angles (cont.):

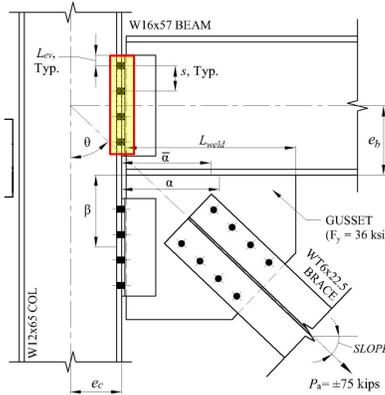
$$q = B \left[\delta \alpha \rho \left(\frac{t}{t_c} \right)^2 \right] \quad (\text{AISC Manual Eq. 9-28})$$

$$= 11.9 \text{ kips} \left[(0.717)(0.441)(1.06) \left(\frac{0.375 \text{ in.}}{0.968 \text{ in.}} \right)^2 \right]$$

$$= 0.599 \text{ kips}$$

$$B_c = T_{bolt} + q = 2.35 \text{ kips} + 0.599 \text{ kips}$$

$$= 2.95 \text{ kips} \leq B = 11.9 \text{ kips} \text{ o.k.}$$



There's always a solution in steel

139

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Prying of Column Flange:

For connections to column webs, there is no tension force on the angle due to the brace force since $H_c = 0$ kips. For this example, which is to a column flange, use the following criteria:

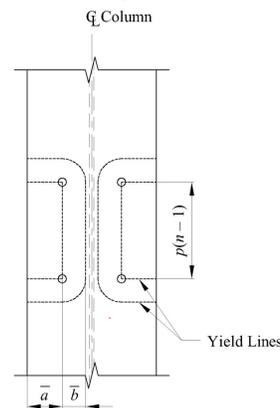
Determine effective flange width

$$p_{eff} = [p(n-1) + \pi \bar{b} + 2\bar{a}] / n$$

(Ref Akbar Tamboli, *Handbook of Steel Connection Design and Details*, 2nd Ed.)

$$p = \text{spacing} = 3 \text{ in.}$$

$$\text{Note: } \bar{a} = a \text{ and } \bar{b} = b$$



(A.P. Mann and L.J. Morris, "Limit Design of Extended End-Plate Connections," *Journal of the Structural Division, ASCE*, Vol. 105, ST3, March 1979)



There's always a solution in steel

140

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Prying of Column Flange (cont.):

$$\bar{b} = (\text{gage} - t_{wc}) / 2$$

$$= (5.5 \text{ in.} - 0.39 \text{ in.}) / 2 = 2.56 \text{ in.}$$

$$\bar{a} = (b_{fc} - \text{gage}) / 2$$

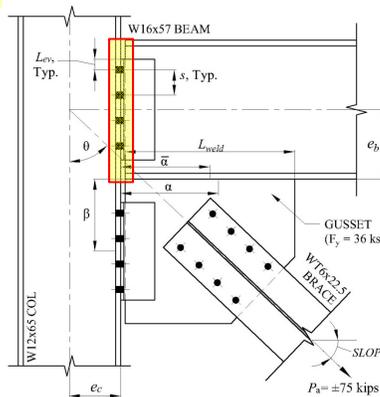
$$= (12 \text{ in.} - 5.5 \text{ in.}) / 2 = 3.25 \text{ in.}$$

$$p_{eff} = [p(n-1) + \pi\bar{b} + 2\bar{a}] / n$$

$$= [(3 \text{ in.})(4-1) + (3.14)(2.56 \text{ in.}) + (2)(3.25 \text{ in.})] / 4$$

$$= 5.88 \text{ in.}$$

Note: use 3" max if at top of column



There's always a solution in steel

141

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Prying of Column Flange (cont.):

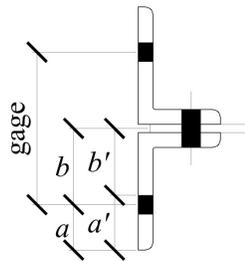
$$T_{bolt} = H_c / 2n = 18.8 \text{ kips} / [(2)(4)] = 2.35 \text{ kips}$$

$$b = \text{gage} / 2 - t_{wc} / 2$$

$$= 5.5 \text{ in.} / 2 - 0.39 \text{ in.} / 2 = 2.56 \text{ in.}$$

$$b' = b - d_b / 2 =$$

$$= 2.56 \text{ in.} - 0.75 \text{ in.} / 2 = 2.18 \text{ in.}$$



There's always a solution in steel

142

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Prying of Column Flange (cont.):

$$a = \min\{(b_{fc} - \text{gage})/2, a \text{ from angle calcs}\}$$

$$= \min\{(12 \text{ in.} - 5.5 \text{ in.})/2, 1.47 \text{ in.}\}$$

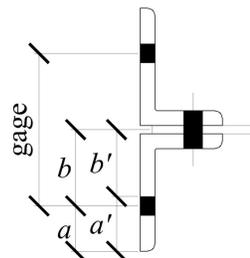
$$= 1.47 \text{ in.}$$

$$a' = a + d_b/2 \leq 1.25b + d_b/2$$

$$= 1.47 \text{ in.} + 0.75 \text{ in.}/2 \leq 1.25(2.56 \text{ in.}) + 0.75 \text{ in.}/2$$

$$= 1.85 \text{ in.} < 3.57 \text{ in.} \text{ Use } 1.85 \text{ in.}$$

$$\rho = b'/a' = 2.18 \text{ in.}/1.85 \text{ in.} = 1.18$$



There's always a solution in steel

143

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Prying of Column Flange (cont.):

$$p = p_{eff} = 5.88 \text{ in.}$$

$$\delta = 1 - d'/p = 1 - (0.8125 \text{ in.}/5.88 \text{ in.})$$

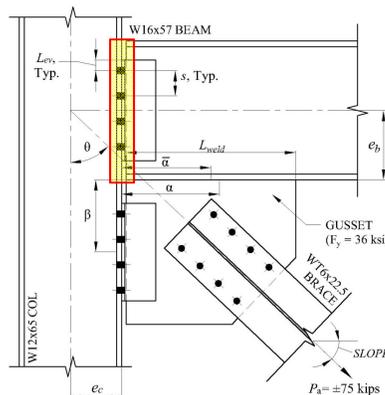
$$= 0.862$$

$$t_c = \sqrt{\frac{\Omega 4 B b'}{p F_u}} \quad (\text{AISC Manual Eq. 9-30a})$$

$$= \sqrt{\frac{1.67(4)(11.9 \text{ kips})(2.18 \text{ in.})}{(5.88 \text{ in.})(65 \text{ ksi})}}$$

$$= 0.673 \text{ in.} > t_f = 0.605 \text{ in.}$$

→ check available strength of bolt including the effects of prying action



There's always a solution in steel

144

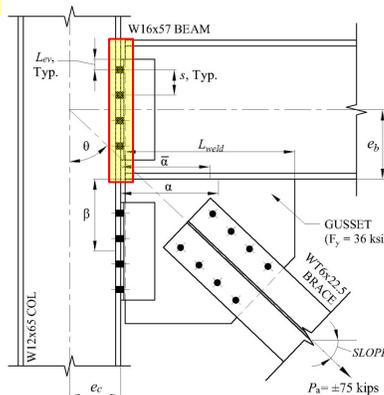
Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Prying of Column Flange
 (cont.):

$$\alpha' = \frac{1}{\delta(1+\rho)} \left[\left(\frac{t_c}{t} \right)^2 - 1 \right] \quad (\text{AISC Manual Eq. 9-35})$$

$$= \frac{1}{0.862(1+1.18)} \left[\left(\frac{0.673 \text{ in.}}{0.605 \text{ in.}} \right)^2 - 1 \right]$$

$$= 0.126 > 0 \text{ and } < 1.0 \rightarrow \text{Eq. 9.33 applies}$$



There's always a solution in steel

145

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Prying of Column Flange
 (cont.):

$$Q = \left(\frac{t}{t_c} \right)^2 (1 + \delta\alpha')$$

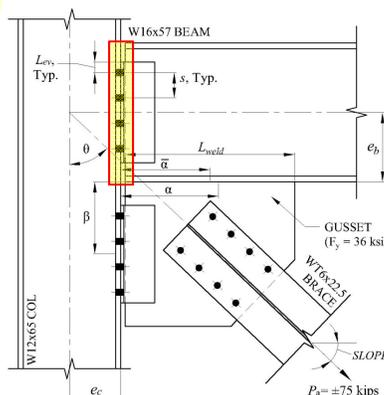
$$= \left(\frac{0.605 \text{ in.}}{0.673 \text{ in.}} \right)^2 [1 + (0.862)(0.126)]$$

$$= 0.896$$

The available strength of bolt including prying is

$$T_{avail} = BQ = (11.9 \text{ kips})(0.896)$$

$$= 10.7 \text{ kips} > T_{bolt} = 2.35 \text{ kips o.k.}$$



There's always a solution in steel

146

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Bolt Bearing/Tearout:

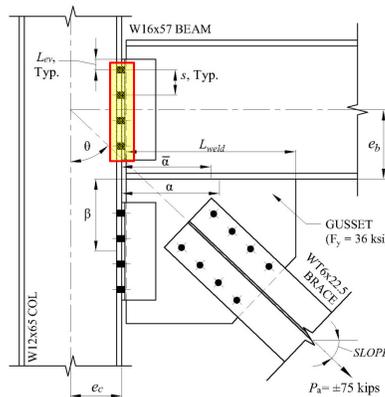
AISC Specification Eq. J3-6a

AISC Bolt Shear:

$$r_v/\Omega = 11.9 \text{ kips}$$

Column Bolt Bearing:

$$\begin{aligned} R_{brg(col)}/\Omega &= 2.4d_b t_f F_u/\Omega \\ &= 2.4(0.75 \text{ in.})(0.605 \text{ in.})(65 \text{ ksi})/2 \\ &= 35.4 \text{ kips} \end{aligned}$$



There's always a solution in steel

147

Example VB Corner Connection, I Beam-to-Column (cont.)

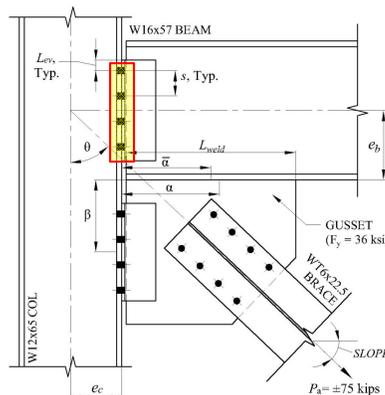
Beam-to-Column – Bolt Bearing (cont.):

Column Bolt Tear Out (Center):

$$\begin{aligned} R_{tear(col_C)}/\Omega &= 1.2(s - d_{h_w}) t_f F_u/\Omega \\ &= 1.2 (3 \text{ in.} - 13/16 \text{ in.}) \\ &\quad \times (0.605 \text{ in.})(65 \text{ ksi})/2 \\ &= 51.6 \text{ kips} \end{aligned}$$

Angle Bolt Bearing:

$$\begin{aligned} R_{brg(L)}/\Omega &= 2.4d_b t_a F_u/\Omega \\ &= 2.4(0.75 \text{ in.})(0.375 \text{ in.})(58 \text{ ksi})/2 \\ &= 19.6 \text{ kips} \end{aligned}$$



There's always a solution in steel

148

Example VB Corner Connection, I Beam-to-Column (cont.)

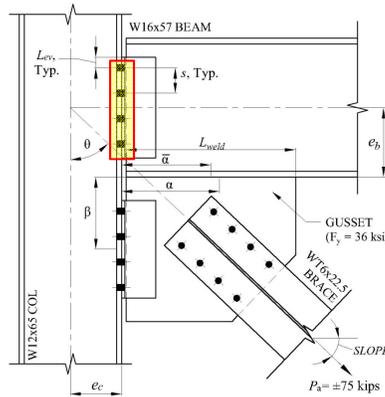
Beam-to-Column – Bolt Bearing (cont.):

Angle Bolt Tear Out (Edge):

$$\begin{aligned}
 R_{tear(L_E)}/\Omega &= 1.2(L_{ev} - d_{h_w}/2)t_a F_u/\Omega \\
 &= 1.2(1.25 \text{ in.} - 13/16 \text{ in.}/2) \\
 &\quad \times (0.375 \text{ in.})(58 \text{ ksi})/2 \\
 &= 11.0 \text{ kips}
 \end{aligned}$$

Angle Bolt Tear Out (Center):

$$\begin{aligned}
 R_{tear(L_C)}/\Omega &= 1.2(s - d_{h_w})t_a F_u/\Omega \\
 &= 1.2(3 \text{ in.} - 13/16 \text{ in.})(0.375 \text{ in.}) \\
 &\quad \times (58 \text{ ksi})/2 \\
 &= 28.6 \text{ kips}
 \end{aligned}$$



There's always a solution in steel

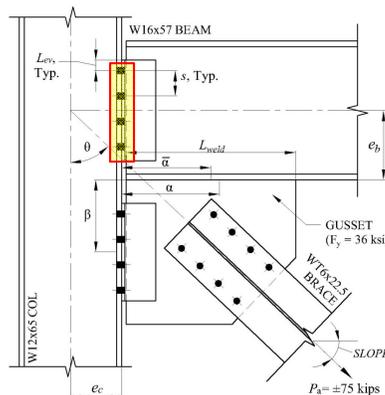
149

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Bolt Bearing (cont.):

$$\begin{aligned}
 R_{n(top)}/\Omega &= \min \{r_v/\Omega, R_{brg(col)}/\Omega, R_{tear(col_C)}/\Omega, \\
 &\quad R_{brg(L)}/\Omega, R_{tear(L_C)}/\Omega\} \\
 &= \min \{11.9 \text{ kips}, 35.4 \text{ kips}, 51.6 \text{ kips}, \\
 &\quad 19.6 \text{ kips}, 28.6 \text{ kips}\} \\
 &= 11.9 \text{ kips}
 \end{aligned}$$

$$\begin{aligned}
 R_{n(center)}/\Omega &= \min \{r_v/\Omega, R_{brg(col)}/\Omega, R_{tear(col_C)}/\Omega, \\
 &\quad R_{brg(L)}/\Omega, R_{tear(L_C)}/\Omega\} \\
 &= \min \{11.9 \text{ kips}, 35.4 \text{ kips}, 51.6 \text{ kips}, \\
 &\quad 19.6 \text{ kips}, 28.6 \text{ kips}\} \\
 &= 11.9 \text{ kips}
 \end{aligned}$$



There's always a solution in steel

150

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Bolt Bearing (cont.):

$$R_{n(bot)}/\Omega = \min \{ r_v/\Omega, R_{brg(col)}/\Omega, R_{tear(col_C)}/\Omega, R_{brg(L)}/\Omega, R_{tear(L_E)}/\Omega \}$$

$$= \min \{ 11.9 \text{ kips}, 35.4 \text{ kips}, 51.6 \text{ kips}, 19.6 \text{ kips}, 11.0 \text{ kips} \}$$

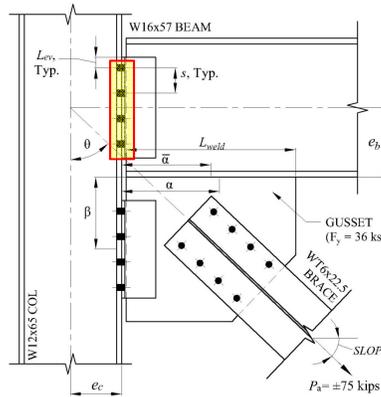
$$= 11.0 \text{ kips}$$

Total Bolt Strength

$$R_n/\Omega = [R_{n(top)}/\Omega + (R_{n(center)}/\Omega)(n - 2) + R_{n(bot)}/\Omega](2 \text{ lines})$$

$$= [11.9 \text{ kips} + (11.9 \text{ kips})(4 - 2) + 11.0 \text{ kips}](2)$$

$$= 93.4 \text{ kips} > V = 67.3 \text{ kips o.k.}$$



There's always a solution in steel

151

Example VB Corner Connection, I Beam-to-Column (cont.)

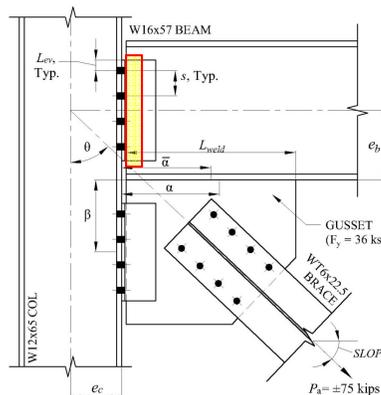
Beam-to-Column – Angle Gross Shear:

AISC Specification Eq. J4-1

$$\frac{R_n}{\Omega} = \frac{0.6F_y A_g}{\Omega}$$

$$= \frac{0.6(36 \text{ ksi})(11.5 \text{ in.})(0.375 \text{ in.})}{1.5}$$

$$= 124 \text{ kips} > V = 67.3 \text{ kips o.k.}$$



There's always a solution in steel

152

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Angle Net Shear:

AISC Specification Eq. J4-4

$$L_{nv} = L_{eff} - n(d_{h,width} + 1/16 \text{ in.})$$

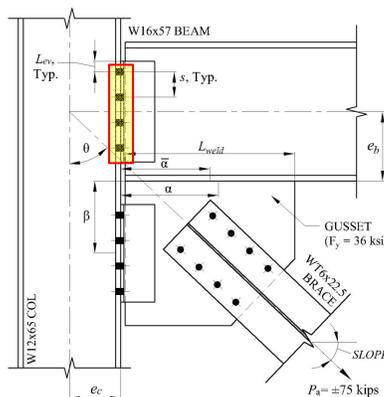
$$= 11.5 \text{ in.} - 4(1\frac{3}{16} \text{ in.} + 1/16 \text{ in.})$$

$$= 8 \text{ in.}$$

$$\frac{R_n}{\Omega} = \frac{0.6F_u A_{nv}}{\Omega}$$

$$= \frac{0.6(58 \text{ ksi})(2)(8 \text{ in.})(0.375 \text{ in.})}{2}$$

$$= 104 \text{ kips} > V = 67.3 \text{ kips o.k.}$$



There's always a solution in steel

153

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Block Shear of Angles

OSL:

AISC Spec Section J4.3 Block Shear Strength

$$\Omega = 2.00$$

$$R_n = 0.6F_u A_{nv} + U_{bs} F_u A_{nt}$$

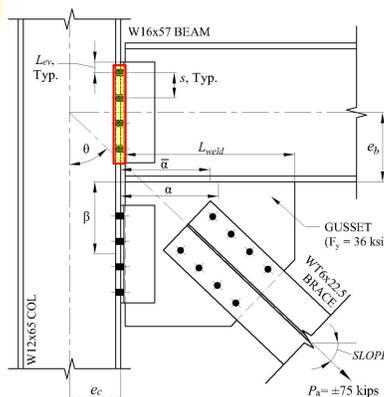
$$\leq 0.6F_y A_{gv} + U_{bs} F_u A_{nt}$$

$$\text{Shear Rupture} = 0.6F_u A_{nv}$$

$$\text{Shear Yield} = 0.6F_y A_{gv}$$

$$\text{Tension Rupture} = F_u A_{nt}$$

$$U_{bs} = 1.0 \text{ for Direct Loaded Connections}$$



There's always a solution in steel

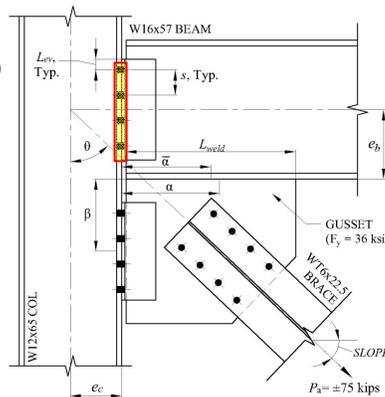
154

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Block Shear of Angles
 OSL (cont.):

$$L_{gv} = L_{ev} + s(n - 1) = 1.25 \text{ in.} + (3 \text{ in.})(4 - 1) = 10.3 \text{ in.}$$

$$L_{nv} = L_{ev} + s(n - 1) - (n - 0.5)(d_h + 1/16 \text{ in.}) - (4 - 0.5)(7/8 \text{ in.}) = 7.19 \text{ in.}$$



There's always a solution in steel

155

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Block Shear of Angles
 OSL (cont.):

$$L_{gt} = L_{eh} = a \text{ from prying calcs} = [2(\text{angle OSL}) + t_w - \text{gage}]/2 = [2(4 \text{ in.}) + 0.43 \text{ in.} - 5.5 \text{ in.}]/2 = 1.47 \text{ in.}$$

$$L_{nt} = L_{eh} - 0.5(\text{hole length} + 1/16 \text{ in.}) = 1.47 \text{ in.} - 0.5(1 \text{ in.} + 1/16 \text{ in.}) = 0.934 \text{ in.}$$

TABLE J3.3
 Nominal Hole Dimensions, in.

Bolt Diameter, in.	Hole Dimensions			
	Standard (Dia.)	Oversize (Dia.)	Short-Slot (Width × Length)	Long-Slot (Width × Length)
1/2	9/16	5/8	9/16 × 1 1/8	9/16 × 1 1/4
5/8	11/16	13/16	11/16 × 7/8	11/16 × 1 3/8
3/4	13/16	15/16	13/16 × 1	13/16 × 1 1/2
7/8	15/16	1 1/16	15/16 × 1 1/8	15/16 × 2 1/8
1	1 1/16	1 1/4	1 1/16 × 1 5/8	1 1/16 × 2 3/8
≥ 1 1/8	d + 1/16	d + 5/16	(d + 1/8) × (d + 3/8)	(d + 1/8) × (2.5 × d)



There's always a solution in steel

156



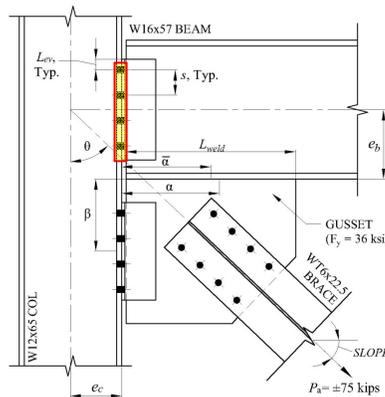
Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Block Shear of Angles
 OSL (cont.):

$$A_{gv} = 2L_{gv}t_a = 2(10.3 \text{ in.})(0.375 \text{ in.}) = 7.73 \text{ in.}^2$$

$$A_{nv} = 2L_{nv}t_a = 2(7.19 \text{ in.})(0.375 \text{ in.}) = 5.39 \text{ in.}^2$$

$$A_{nt} = 2L_{nt}t_a = 2(0.934 \text{ in.})(0.375 \text{ in.}) = 0.701 \text{ in.}^2$$



There's always a solution in steel

157

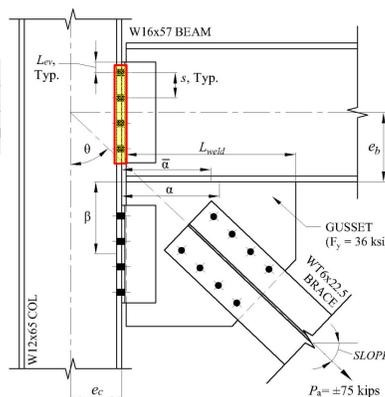
Example VB Corner Connection, I Gusset-to-Column (cont.)

Beam-to-Column – Block Shear of Angles
 OSL (cont.):

$$R_n = \min \left[\begin{array}{l} 0.6(58 \text{ ksi})(5.39 \text{ in.}^2) = 187.57 \text{ kips} \\ 0.6(36 \text{ ksi})(7.73 \text{ in.}^2) = 166.97 \text{ kips} \end{array} \right] + [1(58 \text{ ksi})(0.701 \text{ in.}^2)]$$

$$= 166.97 \text{ kips} + 40.66 \text{ kips} = 207.63 \text{ kips}$$

$$R_n/\Omega = (207.63 \text{ kips})/2 = 104 \text{ kips} > V = 67.3 \text{ kips o.k.}$$



There's always a solution in steel

158

Example VB Corner Connection, I Beam-to-Column (cont.)

**Beam-to-Column – Block Shear of Beam
 Web, Axial:**

AISC Spec Section J4.3 Block Shear Strength

$$\Omega = 2.00$$

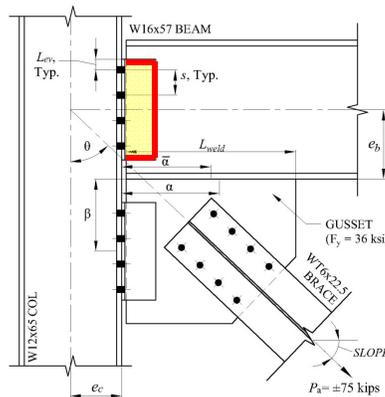
$$R_n = 0.6F_uA_{nv} + U_{bs}F_uA_{nt} \leq 0.6F_yA_{gv} + U_{bs}F_uA_{nt}$$

Shear Rupture = $0.6F_uA_{nv}$

Shear Yield = $0.6F_yA_{gv}$

Tension Rupture = F_uA_{nt}

$U_{bs} = 1.0$ for Direct Loaded Connections



There's always a solution in steel

159

Example VB Corner Connection, I Beam-to-Column (cont.)

**Beam-to-Column – Block Shear of Beam
 Web, Axial (cont.):**

For Axial check:

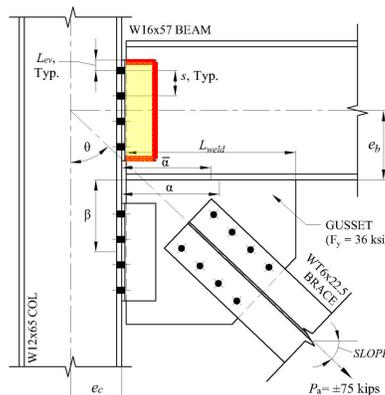
$$L_{gv} = k = 3.5 \text{ in.}$$

$$L_{gt} = 11.5 \text{ in. (length of angle)}$$

$$L_{nv} = L_{gv} = 3.5 \text{ in. (since welded)}$$

$$L_{nt} = L_{gt} = 11.5 \text{ in. (since welded)}$$

Note: The beam is checked for axial load only. Block shear due to shear load is not applicable since top flange is not coped.



There's always a solution in steel

160

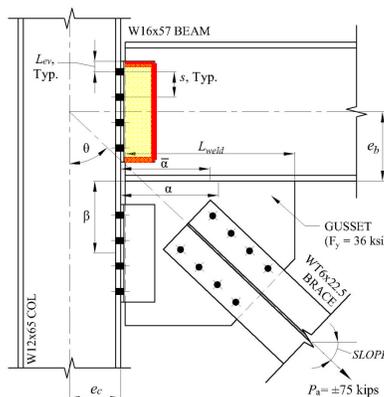
Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Block Shear of Beam Web (cont.):

$$A_{gv} = 2L_{gv}t_w = 2(3.5 \text{ in.})(0.43 \text{ in.}) = 3.01 \text{ in.}^2$$

$$A_{nv} = 2L_{nv}t_w = 2(3.5 \text{ in.})(0.43 \text{ in.}) = 3.01 \text{ in.}^2$$

$$A_{nt} = L_{nt}t_w = (11.5 \text{ in.})(0.43 \text{ in.}) = 4.95 \text{ in.}^2$$



There's always a solution in steel

161

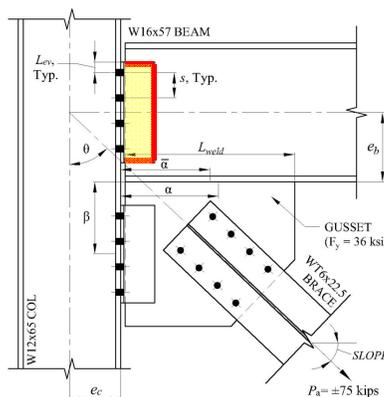
Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Block Shear of Beam Web (cont.):

$$R_n = \min \left[\begin{array}{l} 0.6(65 \text{ ksi})(3.01 \text{ in.}^2) = 117.39 \text{ kips} \\ 0.6(50 \text{ ksi})(3.01 \text{ in.}^2) = 90.30 \text{ kips} \end{array} \right] + [1(65 \text{ ksi})(4.95 \text{ in.}^2)]$$

$$= 90.30 \text{ kips} + 321.75 \text{ kips} = 412.05 \text{ kips}$$

$$R_n/\Omega = (412.05 \text{ kips})/2 = 206 \text{ kips} > H = 18.8 \text{ kips o.k.}$$



There's always a solution in steel

162

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Size Weld:

$$P = \sqrt{V^2 + H^2}$$

$$= \sqrt{(67.3 \text{ kips})^2 + (18.8 \text{ kips})^2}$$

$$= 69.9 \text{ kips}$$

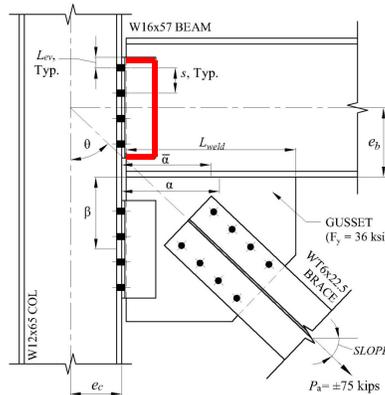
$$\theta = \tan^{-1}(H/V) = \tan^{-1}(18.8 \text{ kips}/67.3 \text{ kips})$$

$$= 15.6^\circ$$

$$l = s(n - 1) + 2L_{ev}$$

$$= (3 \text{ in.})(4 - 1) + 2(1.25 \text{ in.})$$

$$= 11.5 \text{ in.}$$



There's always a solution in steel

The lecture will skip
 to slide 168.

163

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Size Weld (cont.):

$$kl = 3.5 \text{ in.}$$

$$k = kl/l = 3.5 \text{ in.}/11.5 \text{ in.} = 0.304$$

$$x = 0.057$$

$$a = [(al + xl) - xl]/l$$

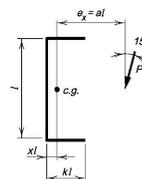
$$= [4 \text{ in.} - (0.057)(11.5 \text{ in.})]/11.5 \text{ in.}$$

$$= 0.29$$

$$C = 2.87 \text{ (AISC Manual Table 8-8 with}$$

$$\text{Angle} = 15^\circ, \text{ round down)}$$

Table 8-8 (continued) AISC Manual
 Coefficients, C,
 for Eccentrically Loaded Weld Groups



a	k											
	0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	1.0	1.2
0.00	1.98	2.47	3.01	3.56	4.10	4.65	5.19	5.74	6.28	6.83	7.37	8.46
0.10	1.90	2.35	2.87	3.41	3.95	4.50	5.05	5.60	6.15	6.70	7.24	8.34
0.15	1.84	2.30	2.79	3.30	3.81	4.33	4.86	5.39	5.92	6.45	6.98	8.06
0.20	1.76	2.21	2.68	3.16	3.65	4.15	4.65	5.16	5.67	6.18	6.69	7.72
0.25	1.65	2.08	2.54	3.00	3.47	3.94	4.42	4.91	5.39	5.89	6.38	7.38
0.30	1.55	1.95	2.39	2.82	3.27	3.72	4.18	4.64	5.11	5.58	6.06	7.03



There's always a solution in steel

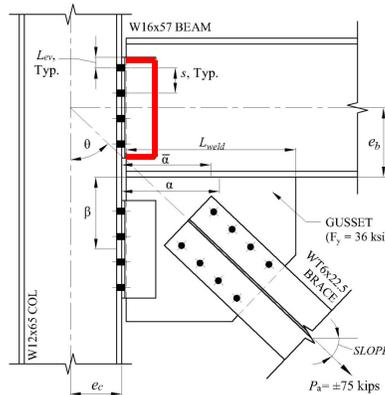
164

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Size Weld (cont.):

$C_1 = 1.0$ for E70 (AISC Manual Table 8-3)

AISC Manual Table 8-3 Electrode Strength Coefficient, C_1		
Electrode	F_{EXX} (ksi)	C_1
E60	60	0.857
E70	70	1.00
E80	80	1.03
E90	90	1.16
E100	100	1.21
E110	110	1.34



There's always a solution in steel

165

Example VB Corner Connection, I Beam-to-Column (cont.)

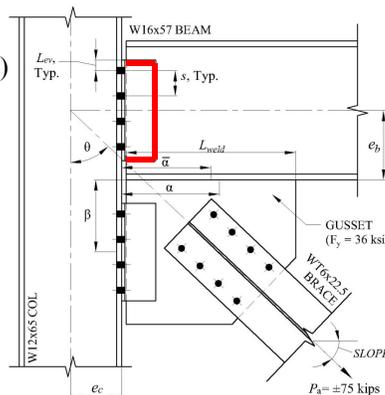
Beam-to-Column – Size Weld (cont.):

$$\begin{aligned}
 D_{min} &= P_c \Omega / (2CC_1L) \\
 &= 69.9 \text{ kips}(2) / ((2)(2.87)(1.0)(11.5 \text{ in.})) \\
 &= 2.12 < 4 \text{ (16}^{\text{th}} \text{ of an inch)} \\
 &\quad \text{1/4" fillet weld o.k.}
 \end{aligned}$$

$$\begin{aligned}
 t_{min} &= 2(0.928D) / (0.6F_u / \Omega) \\
 &= 2(0.928)(2.12) / [(0.6)(65 \text{ ksi} / 2)] \\
 &= 0.202 \text{ in.} > t_w = 0.43 \text{ in. o.k.}
 \end{aligned}$$

Note, the above is same as Manual Eq 9-3:

$$t_{min} = 6.19D / F_u$$



There's always a solution in steel

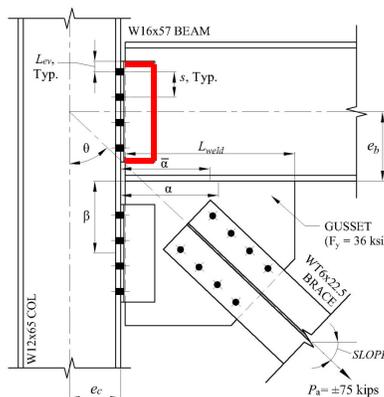
166

Example VB Corner Connection, I Beam-to-Column (cont.)

Beam-to-Column – Size Weld (cont.):

If $t_{min} < t_p$, no reduction necessary.

$$\text{If } t_{min} > t_p, \frac{R_w}{\Omega} = \left(\frac{R_n}{\Omega} \right) \left(\frac{t_p}{t_{min}} \right)$$



There's always a solution in steel

167

Vertical Brace Example

If either the gusset-to-column connection or the beam-to-column cannot be made to work economically, it may be necessary to change the force distribution. This can be done by:

- Changing the dimensions of the gusset plate.
- Using ΔV_b to change the distribution of the vertical brace component.



Practical Connection Design

168

Economy of Vertical Bracing Connections

- Use the Uniform Force Method.
- Use W12 or W14 columns as a minimum where possible.
- Use minimum W18 beams.
- Use same depth beams either side of the column when transfer forces exist.



There's always a solution in steel

169

Economy of Vertical Bracing Connections

- Consider net section capacity when sizing brace members.
- Provide actual loads (tension and compression).



There's always a solution in steel

170



Summary



There's always a solution in steel

171

Summary

- Example of a corner vertical bracing connection was reviewed for a Wind and Low-Seismic condition
 - Began the example with the brace-to-gusset design
 - Gusset dimensions were determined based on the brace-to-gusset connection
 - The gusset-to-column connection including prying action was checked
 - Followed by the gusset-to-beam connection
 - Finally, the beam-to-column connection, also including prying action, was checked



There's always a solution in steel

172





Questions?



There's always a solution in steel

Individual Webinar Registrants

CEU/PDH Certificates

Within 2 business days...

- You will receive an email on how to report attendance from: registration@aisc.org.
- Be on the lookout: Check your spam filter! Check your junk folder!
- Completely fill out online form. Don't forget to check the boxes next to each attendee's name!



Individual Webinar Registrants

CEU/PDH Certificates

Within 2 business days...

- New reporting site (URL will be provided in the forthcoming email).
- Username: Same as AISC website username.
- Password: Same as AISC website password.



8-Session Registrants

CEU/PDH Certificates

One certificate will be issued at the conclusion of
all 8 sessions.



8-Session Registrants

Access to the quiz: Information for accessing the quiz will be emailed to you by Thursday. It will contain a link to access the quiz. EMAIL COMES FROM NIGHTSCHOOL@AISC.ORG

Quiz and Attendance records: Posted Tuesday mornings. www.aisc.org/nightschool
- click on Current Course Details.

Reasons for quiz:

- EEU – must take all quizzes and final to receive EEU
- CEUs/PDHS – If you watch a recorded session you must take quiz for CEUs/PDHS.
- REINFORCEMENT – Reinforce what you learned tonight. Get more out of the course.

NOTE: If you attend the live presentation, you do not have to take the quizzes to receive CEUs/PDHS.



8-Session Registrants

Access to the recording: Information for accessing the recording will be emailed to you by this Wednesday. The recording will be available for two weeks. For 8-session registrants only. EMAIL COMES FROM NIGHTSCHOOL@AISC.ORG.

CEUs/PDHS – If you watch a recorded session you must take AND PASS the quiz for CEUs/PDHS.



There's always a solution in steel.

Thank You

Please give us your feedback!
Survey at conclusion of webinar.

